

# Collections, Part One

# Outline for Today

- ***Parameter Passing in C++***
  - On xeroxes and master copies.
- ***Container Types***
  - Holding lots of pieces of data.
- ***The Vector type***
  - Storing sequences.
- ***Recursion on Vectors***
  - More practice with sequences.

# Parameter Passing in C++

# Make a Prediction!

- Look over this piece of C++ code:

```
void becomeWealthy(int netWorth) {  
    netWorth = 1000000000;  
}  
  
int main() {  
    int value = 137;  
    becomeWealthy(value);  
    cout << value << endl; // <- Here  
    return 0;  
}
```

- What do you think will get printed at the indicated point? Why?

Formulate a hypothesis!

# How it Works

```
int main() {  
    int value = 137;  
    becomeWealthy(value);  
    cout << value << endl;  
    return 0;  
}
```

# How it Works

```
int main() {
    int value = 137;
    becomewealthy(value);
    cout << value << endl;
    return 0;
}
```

# How it Works

```
int main() {  
    int value = 137;  
    becomewealthy(value);  
    cout << value << endl;  
    return 0;  
}
```

137

value

# How it Works

```
int main() {  
    int value = 137;  
    becomeWealthy(value);  
    cout << value << endl;  
    return 0;  
}
```

137

value

# How it Works

```
int main() {  
    int netWorth = 137;  
    void becomeWealthy(int netWorth) {  
        netWorth = 1000000000;  
    }  
}
```

137

137

netWorth

# How it Works

```
int main() {  
    int value = 137;  
    void becomeWealthy(int netWorth) {  
        netWorth = 1000000000;  
    }  
}
```

137

137

netWorth

# How it Works

```
int main() {  
    int value = 127;  
    void becomeWealthy(int netWorth) {  
        netWorth = 1000000000;  
    }  
}
```

137

kaching!

netWorth

# How it Works

```
int main() {  
    int netWorth = 127;  
    void becomeWealthy(int netWorth) {  
        netWorth = 1000000000;  
    }  
}
```

137

kaching!

netWorth

# How it Works

```
int main() {  
    int value = 137;  
    becomeWealthy(value);  
    cout << value << endl;  
    return 0;  
}
```

137

value

# Parameter Passing in C++

- By default, in C++, parameters are passed by value.

```
/* This function gets a copy of the integer passed
 * into it, so we only change our local copy. The
 * caller won't see any changes.
 */
void byValue(int number) {
    number = 137;
}
```

- You can place an ampersand after the type name to take the parameter by reference.

```
/* This function takes its argument by reference, so
 * when the function returns, the int passed in will have
 * been permanently changed.
 */
void byReference(int& number) {
    number = 137;
}
```

# How it Works Now

```
int main() {
    int value = 137;
    becomeWealthy(value);
    cout << value << endl;
    return 0;
}
```

# How it Works Now

```
int main() {
    int value = 137;
    becomewealthy(value);
    cout << value << endl;
    return 0;
}
```

# How it Works Now

```
int main() {  
    int value = 137;  
    becomewealthy(value);  
    cout << value << endl;  
    return 0;  
}
```

137

value

# How it Works Now

```
int main() {  
    int value = 137;  
    becomeWealthy(value);  
    cout << value << endl;  
    return 0;  
}
```

137

value

# How it Works Now

```
int main() {  
    int value = 137;  
    becomeWealthy(value);  
    cout << value << endl;  
}  
void becomeWealthy(int& networth) {  
    networth = 1000000000;  
}
```

The diagram illustrates the state of memory during the execution of the provided C++ code. A large black rectangular box represents the stack frame for the `main` function. Inside this box, the variable `value` is shown with the value 137. A blue rectangular box represents the stack frame for the `becomeWealthy` function. Inside this box, the parameter `networth` is shown with the value 1000000000. A red arrow points from the variable `value` in the `main` frame to the parameter `networth` in the `becomeWealthy` frame, indicating that they share the same memory location. This visualizes how parameters are passed by reference in C++.

# How it Works Now

```
int main() {  
    int value = 137;  
    becomeWealthy(value);  
    cout << value << endl;  
}  
void becomeWealthy(int& networth) {  
    networth = 1000000000;  
}
```

The diagram illustrates the state of variables in memory. A blue box labeled '137' represents the initial value of 'value'. A red arrow points from this box to a vertical grey bar labeled 'value' at its top. Inside a larger black-bordered box, another blue box labeled '1000000000' represents the modified value of 'networth' passed by reference. A red arrow points from this box to a vertical grey bar labeled 'networth' at its top. The code shows that the original variable 'value' retains its initial value of 137, while the variable 'networth' is modified to 1000000000.

# How it Works Now

```
int main() {  
    int value = 137;  
    becomeWealthy(value);  
    cout << value << endl;  
}  
void becomeWealthy(int& networth) {  
    networth = 1000000000;  
}
```

The diagram illustrates the state of variables during the execution of the code. A grey bar at the bottom represents the stack, and a white box above it represents the heap. In the main function's scope (left), there is a local variable `value` (grey box) containing the value 137. In the `becomeWealthy` function's scope (right), there is a parameter `networth` (grey box) pointing to the same memory location as `value`. A blue box highlights the assignment statement `networth = 1000000000;`. After this assignment, a red arrow labeled "kaching!" points from the `value` variable to the new value 1000000000, indicating that the original variable has been modified.

# How it Works Now

```
int main() {  
    int value = 137;  
    becomeWealthy(value);  
    cout << value << endl;  
}  
void becomeWealthy(int& netWorth) {  
    netWorth = 1000000000;  
}
```

The diagram illustrates the state of variables during the execution of the code. A blue box highlights the line `becomeWealthy(value);`. To its right, a red arrow points from the word `value` to a vertical grey bar representing memory. A blue box labeled `kaching!` is positioned above the memory bar. The `netWorth` parameter in the `becomeWealthy` function is also labeled `value`, indicating that the local variable `netWorth` shadows the global `value`. The `netWorth` variable is shown as a large white area within the `becomeWealthy` function's scope, representing its mutated state.

# How it Works Now

```
int main() {  
    int value = 137;  
    becomeWealthy(value);  
    cout << value << endl;  
    return 0;  
}
```

kaching!

value

# Make a Prediction!

- Look over this piece of C++ code:

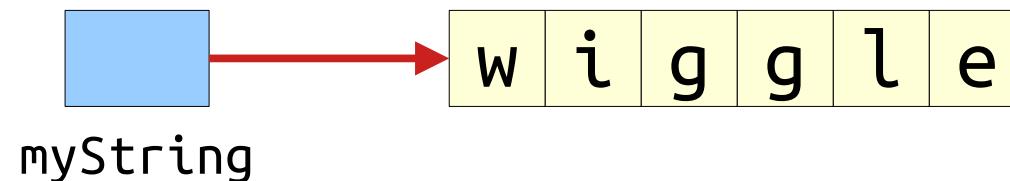
```
void gollyGee(string text) {  
    text[0] = 'g';  
}  
  
int main() {  
    string message = "wiggle";  
    gollyGee(message);  
    cout << message << endl; // <-- Here  
    return 0;  
}
```

- What do you think will get printed at the indicated point? Why?

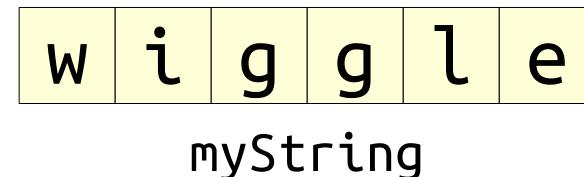
Formulate a hypothesis!

# Strings in C++

- In Python, Java, and JavaScript, string variables are not the strings themselves. They're pointers to those strings.



- In C++, a variable of type `string` is an actual, concrete, honest-to-goodness string.



# How it Works

```
int main() {  
    string message = "wiggle";  
    gollyGee(message);  
    cout << message << endl;  
    return 0;  
}
```

# How it Works

```
int main() {
    string message = "wiggle";
    gollyGee(message);
    cout << message << endl;
    return 0;
}
```

# How it Works

```
int main() {  
    string message = "wiggle";  
    gollyGee(message);  
    cout << message << endl;  
    return 0;  
}
```

wiggle

message

# How it Works

```
int main() {  
    string message = "wiggle";  
    gollyGee(message);  
    cout << message << endl;  
    return 0;  
}
```

wiggle

message

# How it Works

```
int main() {  
    string text = "Hello".  
    wiggle  
    void gollyGee(string text) {  
        text[0] = 'g';  
        wiggle  
    }  
}  
text
```

# How it Works

```
int main() {  
    string text = "Hello".  
    wiggle  
    void gollyGee(string text) {  
        text[0] = 'g';  
        wiggle  
    }  
}  
text
```

# How it Works

```
int main() {  
    string text = "wibble".  
    wiggle(text);  
    giggle(text);  
}  
  
void gollyGee(string text) {  
    text[0] = 'g';  
}
```

# How it Works

```
int main() {  
    string text = "wibble".  
    wiggle.  
    void gollyGee(string text) {  
        text[0] = 'g';  
    }  
}
```

wiggle

giggle

text

# How it Works

```
int main() {  
    string message = "wiggle";  
    gollyGee(message);  
    cout << message << endl;  
    return 0;  
}
```

wiggle

value

# Adding An Ampersand

# How it Works Now

```
int main() {  
    string message = "wiggle";  
    gollyGee(message);  
    cout << message << endl;  
    return 0;  
}
```

# How it Works Now

```
int main() {
    string message = "wiggle";
    gollyGee(message);
    cout << message << endl;
    return 0;
}
```

# How it Works Now

```
int main() {  
    string message = "wiggle";  
    gollyGee(message);  
    cout << message << endl;  
    return 0;  
}
```

wiggle

message

# How it Works Now

```
int main() {  
    string message = "wiggle";  
    gollyGee(message);  
    cout << message << endl;  
    return 0;  
}
```

wiggle

message

# How it Works Now

```
int main() {  
    string message = "wiggle";  
    gollyGee(message);  
    cout << message << endl;  
}  
  
void gollyGee(string& text) {  
    text[0] = 'g';  
}
```

wiggle

message

text

# How it Works Now

```
int main() {
    string message = "wiggle";
    gollyGee(message);
    cout << message << endl;
}

void gollyGee(string& text) {
    text[0] = 'g';
}
```

wiggle

message

text



# How it Works Now

```
int main() {
    string message = "wiggle";
    gollyGee(message);
    cout << message << endl;
}

void gollyGee(string& text) {
    text[0] = 'g';
}
```

The diagram illustrates the state of memory for the variable `message`. A blue box highlights the assignment statement `text[0] = 'g';`. A red arrow points from this box to a blue box labeled `giggle`, which is the mutated value of the string. Another red arrow points from the original `message` variable to a blue box labeled `text`, indicating that they now point to the same memory location.

# How it Works Now

```
int main() {
    string message = "wiggle";
    gollyGee(message);
    cout << message << endl;
}

void gollyGee(string& text) {
    text[0] = 'g';
}
```

The diagram illustrates the state of variables in memory. In the main function, a variable named `message` is assigned the value "wiggle". This variable is highlighted with a blue box. In the `gollyGee` function, a parameter named `text` receives a reference to the same `message` variable. Inside the function, the first character of `text` is modified to 'g', changing the value to "giggle". An arrow points from the `message` variable in the main function to the `giggle` value in the `text` parameter of the `gollyGee` function, demonstrating that the modification is reflected back in the original variable.

# How it Works Now

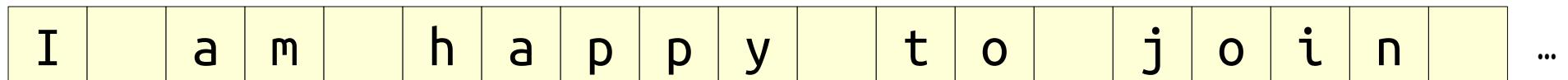
```
int main() {  
    string message = "wiggle";  
    gollyGee(message);  
    cout << message << endl;  
    return 0;  
}
```

giggle

message

# A Question of Speed

- When working with strings, pass-by-value is slower than pass-by-reference because of the cost of copying the string.



- ***General principle:*** When passing a string into a function, use pass-by-reference unless you actually want a copy of the string.

# Do You Trust Me?

- Suppose you've written the next Great American Novel and the single, sole copy is stored in the variable

```
string myMasterpiece;
```

- You see a function with this signature:  
**void** totallyNotSketchy(string& text);
- Would you make this call?

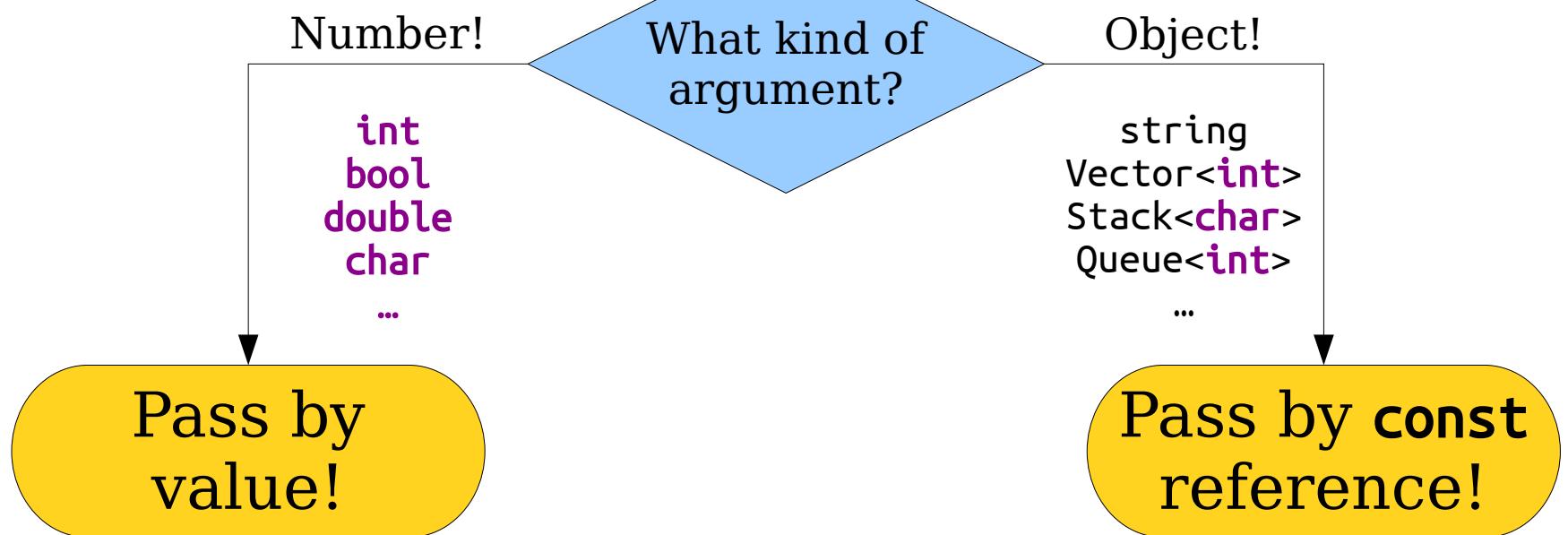
```
totallyNotSketchy(myMasterpiece);
```

# Pass-by-const-Reference

- If you want to look at, but not modify, a function parameter, pass it by ***const reference***:
  - The “by reference” part avoids a copy.
  - The “**const**” (constant) part means that the function can’t change that argument.
- For example:

```
void proofreadLongEssay(const string& essay) {  
    /* can read, but not change, the essay. */  
}
```

This is the general convention used in C++ programming. Please feel free to ask questions about this over the course of the quarter!



# Container Types

# Container Types

- A ***collection class*** (also called an ***abstract data type*** or ***container class***) is a data type used to store and organize data in some form.
  - These are things like arrays, lists, maps, dictionaries, etc.
- Our next three lectures exploring collections and how to use them appropriately.
- Later, we'll analyze their efficiencies. For now, let's just focus on how to use them.

# Vector

# Vector

- A **Vector** is a collection class representing a list of things.
- It's similar to Java's `ArrayList`, JavaScript's arrays, and Python's lists.
- To make a Vector, use this syntax:

`Vector<type> name;`

- All elements of a Vector have to have the same type. You specify that type by placing it in <angle brackets> after the word `Vector`.

# Vector in Action

```
/*      Stanford C++ Version      */
Vector<int> v = { 1, 3, 7 };

v += 271;
cout << v[0] << endl;
cout << v[v.size() - 1] << endl;
Vector<int> first = v.subList(0, 2);
Vector<int> last  = v.subList(2);

v.remove(0);
```

```
"""      Python Version      """
v = [1, 3, 7]

v.append(271)
print(v[0])
print(v[-1])
first = v[0:2]
last  = v[2:]

del v[0]
```

```
/*      Java Version      */
List<> v = new ArrayList<Integer>();
v.add(1); v.add(3); v.add(7);

v.add(271);

System.out.println(v.get(0));
System.out.println(v.get(v.size()-1));

List<Integer> first = v.subList(0, 2);
List<Integer> last  = v.subList(2);

v.remove(0);
```

```
//      JavaScript Version
let v = [1, 3, 7];

v.push(271);
console.log(v[0]);
console.log(v[v.length - 1]);

let first = v.slice(0, 2);
let last  = v.slice(2);

v.splice(0, 0);
```

```
/*      Stanford C++ Version      */
Vector<int> v = { 1, 3, 7 };

v += 271;
cout << v[0] << endl;
cout << v[v.size() - 1] << endl;
Vector<int> first = v.subList(0, 2);
Vector<int> last  = v.subList(2);

v.remove(0);
```

```
""" Python Version """
v = [1, 3, 7]

v.append(271)
print(v[0])
print(v[-1])
first = v[0:2]
last  = v[2:]

del v[0]
```

```
/*      Java Version      */
List<> v = new ArrayList<Integer>();
v.add(1); v.add(3); v.add(7);

v.add(271);

System.out.println(v.get(0));
System.out.println(v.get(v.size()-1));

List<Integer> first = v.subList(0, 2);
List<Integer> last  = v.subList(2);

v.remove(0);
```

```
//  JavaScript Version
let v = [1, 3, 7];

v.push(271);
console.log(v[0]);
console.log(v[v.length - 1]);

let first = v.slice(0, 2);
let last  = v.slice(2);

v.splice(0, 0);
```

```

/*      Stanford C++ Version      */
Vector<int> v = { 1, 3, 7 };

v += 271;
cout << v[0] << endl;
cout << v[v.size() - 1] << endl;
Vector<int> first = v.subList(0, 2);
Vector<int> last  = v.subList(2);

v.remove(0);

```

```

"""" Python Version """
v = [1, 3, 7]

v.append(271)
print(v[0])
print(v[-1])
first = v[0:2]
last  = v[2:]


```

Note the use of curly braces rather than square brackets here.

```

/*      Java Version      */
List<> v = new ArrayList<Integer>();
v.add(1); v.add(3); v.add(7);

v.add(271);

System.out.println(v.get(0));
System.out.println(v.get(v.size()-1));

List<Integer> first = v.subList(0, 2);
List<Integer> last  = v.subList(2);

v.remove(0);

```

```

let v = [1, 3, 7];

v.push(271);

console.log(v[0]);
console.log(v[v.length - 1]);

let first = v.slice(0, 2);
let last  = v.slice(2);

v.splice(0, 0);

```

```
/*      Stanford C++ Version      */
Vector<int> v = { 1, 3, 7 };

v += 271; ←

cout << v[0] << endl;
cout << v[v.size() - 1] << endl;

Vector<int> first = v.subList(0, 2);
Vector<int> last  = v.subList(2);

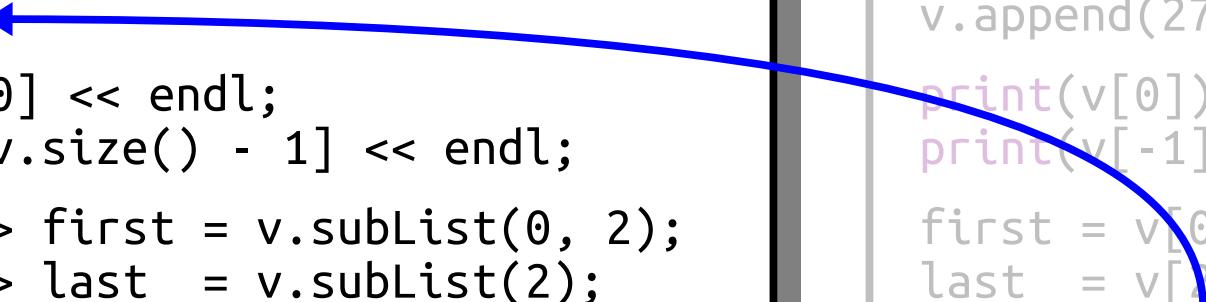
v.remove(0);
```

```
"""\n      Python Version\n"""
v = [1, 3, 7]

v.append(271)

print(v[0])
print(v[-1])

first = v[0:2]
last  = v[2:]


```

We append elements  
using the `+=`  
operator.

```
/*      Java Version      */
List<> v = new ArrayList<Integer>();
v.add(1); v.add(3); v.add(7);

v.add(271);

System.out.println(v.get(0));
System.out.println(v.get(v.size()-1));

List<Integer> first = v.subList(0, 2);
List<Integer> last  = v.subList(2);

v.remove(0);
```

```
let v = [1, 3, 7];

v.push(271);

console.log(v[0]);
console.log(v[v.length - 1]);

let first = v.slice(0, 2);
let last  = v.slice(2);

v.splice(0, 0);
```

```
/*      Stanford C++ Version      */
Vector<int> v = { 1, 3, 7 };

v += 271;

cout << v[0] << endl; ←
cout << v[v.size() - 1] << endl;

Vector<int> first = v.subList(0, 2);
Vector<int> last  = v.subList(2);

v.remove(0);
```

```
/*      Java Version      */
List<> v = new ArrayList<Integer>();
v.add(1); v.add(3); v.add(7);

v.add(271);

System.out.println(v.get(0));
System.out.println(v.get(v.size()-1));

List<Integer> first = v.subList(0, 2);
List<Integer> last  = v.subList(2);

v.remove(0);
```

```
"""" Python Version """
v = [1, 3, 7]

v.append(271)

print(v[0])
print(v[-1])

first = v[0:2]
last  = v[2:]
```

We select individual elements out of a Vector using square brackets.

Everything is zero-indexed.

```
v.push(271);

console.log(v[0]);
console.log(v[v.length - 1]);

let first = v.slice(0, 2);
let last  = v.slice(2);

v.splice(0, 0);
```

```
/*      Stanford C++ Version      */
Vector<int> v = { 1, 3, 7 };

v += 271;

cout << v[0] << endl;
cout << v[v.size() - 1] << endl; ←

Vector<int> first = v.subList(0, 2);
Vector<int> last  = v.subList(2);

v.remove(0);
```

```
/*      Java Version      */
List<> v = new ArrayList<Integer>();
v.add(1); v.add(3); v.add(7);

v.add(271);

System.out.println(v.get(0));
System.out.println(v.get(v.size()-1));

List<Integer> first = v.subList(0, 2);
List<Integer> last  = v.subList(2);

v.remove(0);
```

```
"""" Python Version """
v = [1, 3, 7]

v.append(271)

print(v[0])
print(v[-1])

first = v[0:2]
last  = v[2:]
```

C++ doesn't support negative array indices to mean "count from the back." We have to do some math to find the index of the last element.

We use the syntax `v.size()` to get the length of a Vector.

```
v.splice(0, 0);
```

```
/*      Stanford C++ Version      */
Vector<int> v = { 1, 3, 7 };

v += 271;
cout << v[0] << endl;
cout << v[v.size() - 1] << endl;
Vector<int> first = v.subList(0, 2);
Vector<int> last  = v.subList(2);
v.remove(0);
```

```
"""\n      Python Version\n"""
v = [1, 3, 7]

v.append(271)

print(v[0])
print(v[-1])

first = v[0:2]
last  = v[2:]

del v[0]
```

```
/*      Java Version      */
List<> v = new ArrayList<Integer>();
v.add(1); v.add(3); v.add(7);
v.add(271);

System.out.println(v.get(0));
System.out.println(v.get(v.size()-1));
List<Integer> first = v.subList(0, 2);
List<Integer> last  = v.subList(2);
v.remove(0);
```

/\* JavaScrip Version \*/
The subList member function  
is used to get a subrange  
of the subList. Here, first  
will be the first two  
elements of the Vector, and  
last will be the list starting  
at position 2.

```
/*      Stanford C++ Version      */
Vector<int> v = { 1, 3, 7 };

v += 271;
cout << v[0] << endl;
cout << v[v.size() - 1] << endl;
Vector<int> first = v.subList(0, 2);
Vector<int> last  = v.subList(2);
v.remove(0);
```

```
"""\n      Python Version\n"""
v = [1, 3, 7]

v.append(271)
print(v[0])
print(v[-1])
first = v[0:2]
last  = v[2:]
del v[0]
```

```
/*      Java Version      */
List<> v = new ArrayList<Integer>();
v.add(1); v.add(3); v.add(7);
v.add(271);

System.out.println(v.get(0));
System.out.println(v.get(v.size()-1));

List<Integer> first = v.subList(0, 2);
List<Integer> last  = v.subList(2);
v.remove(0);
```

// JavaScript Version

We can use the remove member function to remove the element at a given index.

```
let first = v.slice(0, 2);
let last  = v.slice(2);

v.splice(0, 0);
```

```
/*      Stanford C++ Version      */
Vector<int> v = { 1, 3, 7 };

v += 271;
cout << v[0] << endl;
cout << v[v.size() - 1] << endl;
Vector<int> first = v.subList(0, 2);
Vector<int> last  = v.subList(2);

v.remove(0);
```

```
"""      Python Version      """
v = [1, 3, 7]

v.append(271)
print(v[0])
print(v[-1])
first = v[0:2]
last  = v[2:]

del v[0]
```

```
/*      Java Version      */
List<> v = new ArrayList<Integer>();
v.add(1); v.add(3); v.add(7);

v.add(271);

System.out.println(v.get(0));
System.out.println(v.get(v.size()-1));

List<Integer> first = v.subList(0, 2);
List<Integer> last  = v.subList(2);

v.remove(0);
```

```
//      JavaScript Version
let v = [1, 3, 7];

v.push(271);
console.log(v[0]);
console.log(v[v.length - 1]);

let first = v.slice(0, 2);
let last  = v.slice(2);

v.splice(0, 0);
```



```
/*      Stanford C++ Version      */
Vector<string> v = { "A", "B", "C" };

/* Counting for loop. */
for (int i = 0; i < v.size(); i++) {
    cout << v[i] << endl;
}

/* Range-based for loop. */
for (string elem: v) {
    cout << elem << endl;
}
```

```
"""\n      Python Version\n"""
v = ["A", "B", "C"]

# Counting for loop.
for i in range(len(v)):
    print(v[i])

# Range-based for loop.
for elem in v:
    print(elem)
```

```
/*      Java Version      */
List<> v = new ArrayList<String>();
v.add("A"); v.add("B"); v.add("C");

/* Counting for loop. */
for (int i = 0; i < v.size(); i++) {
    System.out.println(v[i]);
}

/* Range-based for loop. */
for (String elem: v) {
    System.out.println(elem);
}
```

```
//      JavaScript Version
let v = ["A", "B", "C"];

// Counting for loop.
for (let i in v) {
    console.log(v[i]);
}

// Range-based for loop.
for (let elem of v) {
    console.log(elem);
}
```

```
/*      Stanford C++ Version      */
Vector<string> v = { "A", "B", "C" };

/* Counting for loop. */
for (int i = 0; i < v.size(); i++) {
    cout << v[i] << endl;
}

/* Range-based for loop. */
for (string elem: v) {
    cout << elem << endl;
}
```

```
"""      Python Version      """
v = ["A", "B", "C"]

# Counting for loop.
for i in range(len(v)):
    print(v[i])

# Range-based for loop.
for elem in v:
    print(elem)
```

```
/*      Java Version      */
List<> v = new ArrayList<String>();
v.add("A"); v.add("B"); v.add("C");

/* Counting for loop. */
for (int i = 0; i < v.size(); i++) {
    System.out.println(v[i]);
}

/* Range-based for loop. */
for (String elem: v) {
    System.out.println(elem);
}
```

```
//      JavaScript Version      "
let v = ["A", "B", "C"];

// Counting for loop.
for (let i in v) {
    console.log(v[i]);
}

// Range-based for loop.
for (let elem of v) {
    console.log(elem);
}
```

```
/*      Stanford C++ Version      */
Vector<string> v = { "A", "B", "C" };

/* Counting for loop. */
for (int i = 0; i < v.size(); i++) { ←
    cout << v[i] << endl;
}

/* Range-based for loop. */
for (string elem: v) {
    cout << elem << endl;
}
```

```
"""      Python Version      """
v = ["A", "B", "C"]

# Counting for loop.
for i in range(len(v)):
    print(v[i])

# Range-based for loop.
for elem in v:
    print(elem)
```

```
/*      Java Version      */
List<> v = new ArrayList<String>();
v.add("A"); v.add("B"); v.add("C");

/* Counting for loop. */
for (int i = 0; i < v.size(); i++) {
    System.out.println(v[i]);
}

/* Range-based for loop. */
for (String elem: v) {
    System.out.println(elem);
}
```

We can iterate over the elements of a Vector by counting upward from 0 (inclusive) to its size (exclusive) and accessing each element.

```
for (int i = 0; i < v.size(); i++) {
    console.log(v[i]);
}
```

```
/*      Stanford C++ Version      */
Vector<string> v = { "A", "B", "C" };

/* Counting for loop. */
for (int i = 0; i < v.size(); i++) {
    cout << v[i] << endl;
}

/* Range-based for loop. */
for (string elem: v) { ←
    cout << elem << endl;
}
```

```
"""      Python Version      """
v = ["A", "B", "C"]

# Counting for loop.
for i in range(len(v)):
    print(v[i])

# Range-based for loop.
for elem in v:
    print(elem)
```

```
/*      Java Version      */
List<> v = new ArrayList<String>();
v.add("A"); v.add("B"); v.add("C");

/* Counting for loop. */
for (int i = 0; i < v.size(); i++) {
    System.out.println(v[i]);
}

/* Range-based for loop. */
for (String elem: v) {
    System.out.println(elem);
}
```

We can also use this loop structure, which visits each element of the Vector in the order in which they appear.

```
// Range-based for loop.
for (let elem of v) {
    console.log(elem);
}
```

```
/*      Stanford C++ Version      */
Vector<string> v = { "A", "B", "C" };

/* Counting for loop. */
for (int i = 0; i < v.size(); i++) {
    cout << v[i] << endl;
}

/* Range-based for loop. */
for (string elem: v) {
    cout << elem << endl;
}
```

```
"""\n      Python Version\n"""
v = ["A", "B", "C"]

# Counting for loop.
for i in range(len(v)):
    print(v[i])

# Range-based for loop.
for elem in v:
    print(elem)
```

```
/*      Java Version      */
List<> v = new ArrayList<String>();
v.add("A"); v.add("B"); v.add("C");

/* Counting for loop. */
for (int i = 0; i < v.size(); i++) {
    System.out.println(v[i]);
}

/* Range-based for loop. */
for (String elem: v) {
    System.out.println(elem);
}
```

```
//      JavaScript Version
let v = ["A", "B", "C"];

// Counting for loop.
for (let i in v) {
    console.log(v[i]);
}

// Range-based for loop.
for (let elem of v) {
    console.log(elem);
}
```

To read more about the Vector and how to use it, check out the

**Stanford C++ Library Documentation**

up on the course website.

# Make a Prediction!

- Look over this piece of C++ code:

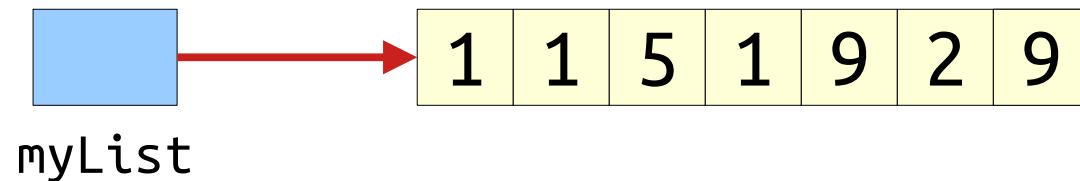
```
void dream(Vector<int> numbers) {  
    numbers[1] = 1963;  
}  
  
int main() {  
    Vector<int> values = { 1929, 1955, 1964 };  
    dream(values);  
    cout << values << endl; // <-- Here  
    return 0;  
}
```

- What do you think will get printed at the indicated point? Why?

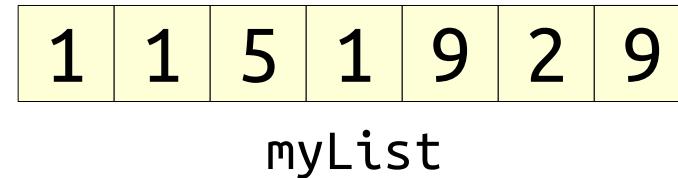
Formulate a hypothesis!

# Objects in C++

- In Python, Java, and JavaScript, object variables are not the objects themselves. They're pointers to those objects:



- In C++, a variable of object type is an actual, concrete, honest-to-goodness object.



# How it Works

```
int main() {
    Vector<int> values = { 1929, 1955, 1964 };
    dream(values);
    cout << values << endl;
    return 0;
}
```

# How it Works

```
int main() {
    Vector<int> values = { 1929, 1955, 1964 };
    dream(values);
    cout << values << endl;
    return 0;
}
```

# How it Works

```
int main() {  
    Vector<int> values = { 1929, 1955, 1964 };  
    dream(values);  
    cout << values << endl;  
    return 0;  
}
```

1929	1955	1964
------	------	------

values

# How it Works

```
int main() {  
    Vector<int> values = { 1929, 1955, 1964 };  
    dream(values);  
    cout << values << endl;  
    return 0;  
}
```

1929	1955	1964
------	------	------

values

# How it Works

i

```
void dream(Vector<int> numbers) {  
    numbers[1] = 1963;  
}
```

1929	1955	1964
------	------	------

numbers

# How it Works

i

```
void dream(Vector<int> numbers) {  
    numbers[1] = 1963;  
}
```

1929	1955	1964
------	------	------

numbers

# How it Works

i

```
void dream(Vector<int> numbers) {  
    numbers[1] = 1963;  
}
```

1929	1963	1964
------	------	------

numbers

# How it Works

i

```
void dream(Vector<int> numbers) {  
    numbers[1] = 1963;  
}
```

1929	1963	1964
------	------	------

numbers

# How it Works

```
int main() {  
    Vector<int> values = { 1929, 1955, 1964 };  
    dream(values);  
    cout << values << endl;  
    return 0;  
}
```

1929	1955	1964
------	------	------

values

# How it Works Now

# How it Works Now

```
int main() {
    Vector<int> values = { 1929, 1955, 1964 };
    dream(values);
    cout << values << endl;
    return 0;
}
```

# How it Works Now

```
int main() {
    Vector<int> values = { 1929, 1955, 1964 };
    dream(values);
    cout << values << endl;
    return 0;
}
```

# How it Works Now

```
int main() {  
    Vector<int> values = { 1929, 1955, 1964 };  
    dream(values);  
    cout << values << endl;  
    return 0;  
}
```

1929	1955	1964
------	------	------

values

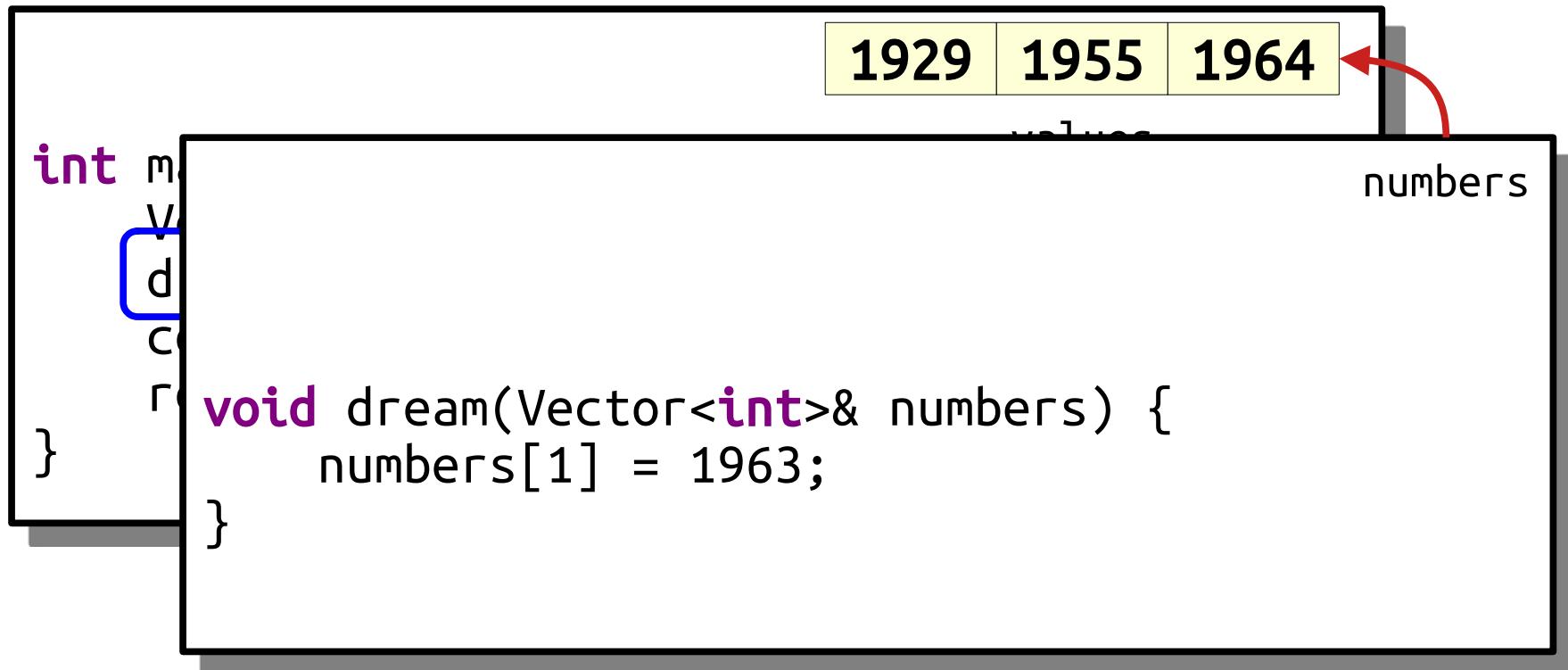
# How it Works Now

```
int main() {  
    Vector<int> values = { 1929, 1955, 1964 };  
    dream(values);  
    cout << values << endl;  
    return 0;  
}
```

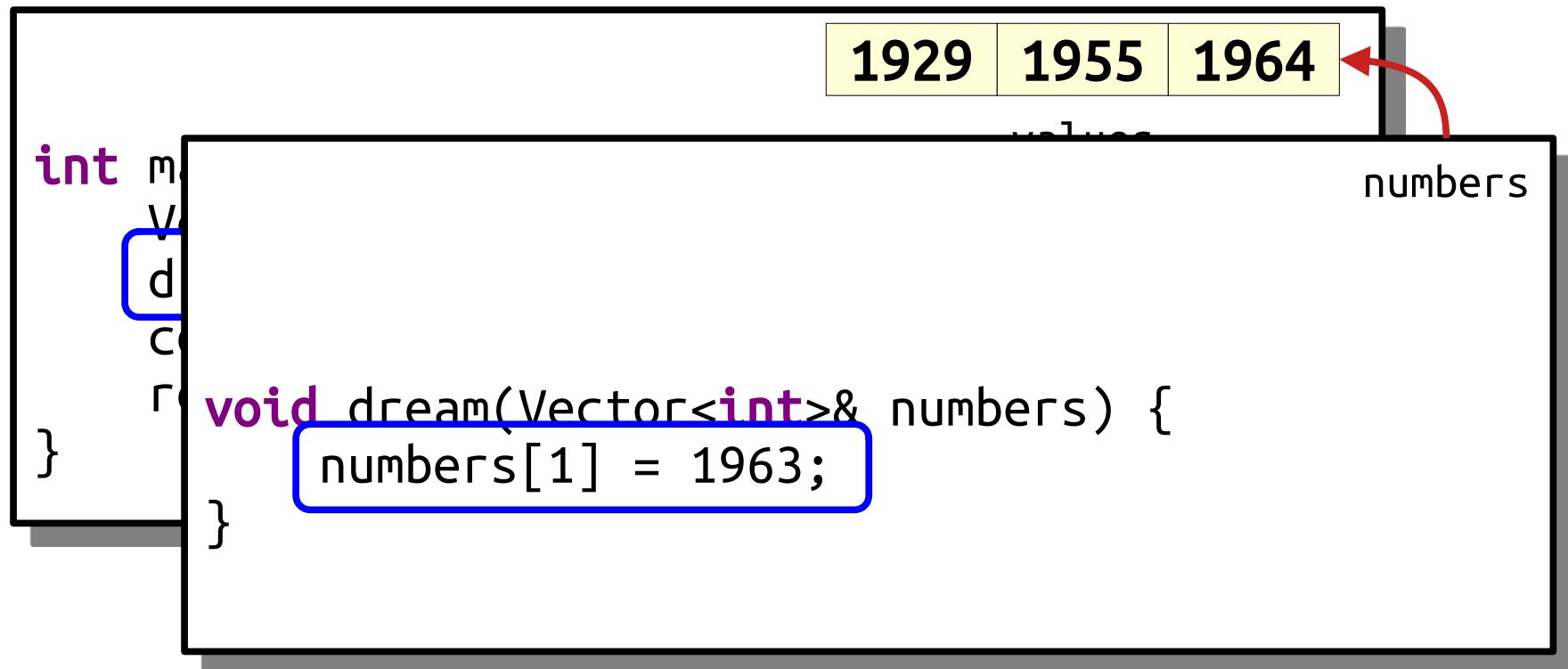
1929	1955	1964
------	------	------

values

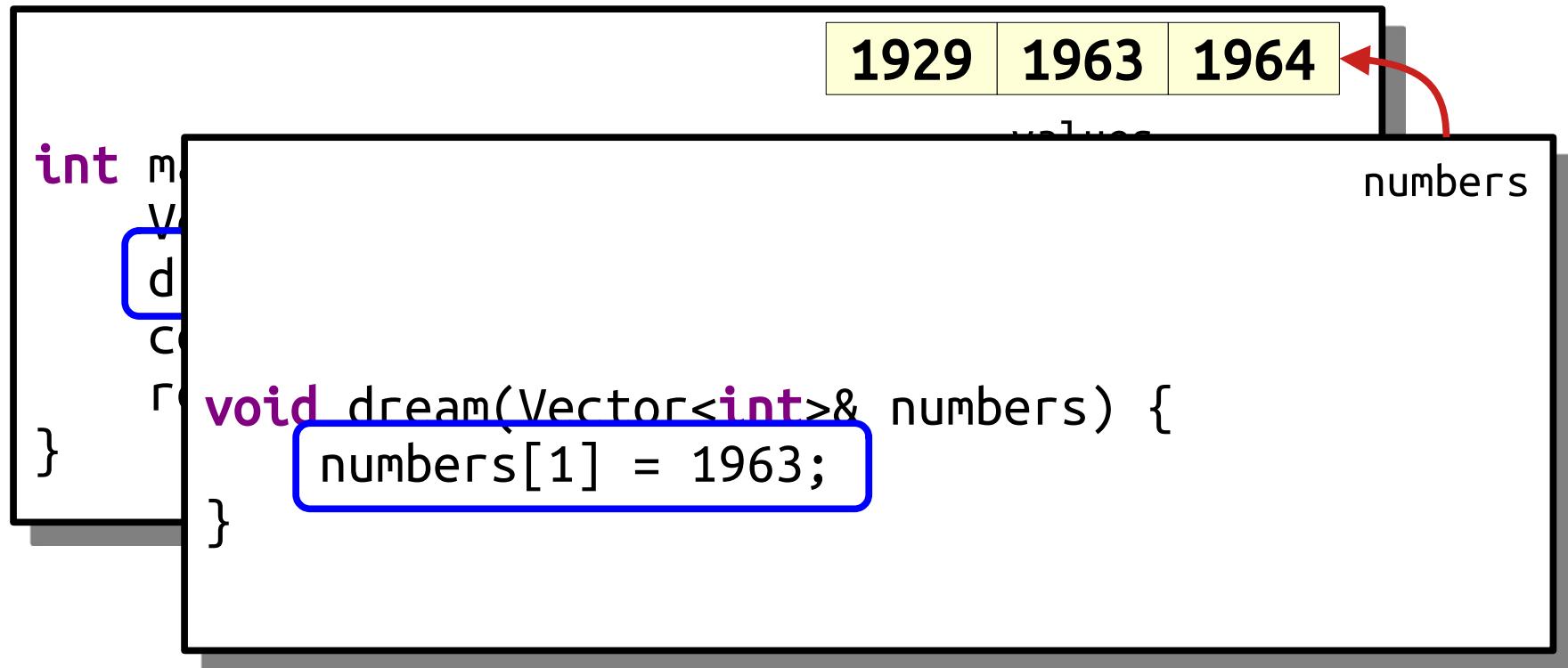
# How it Works Now



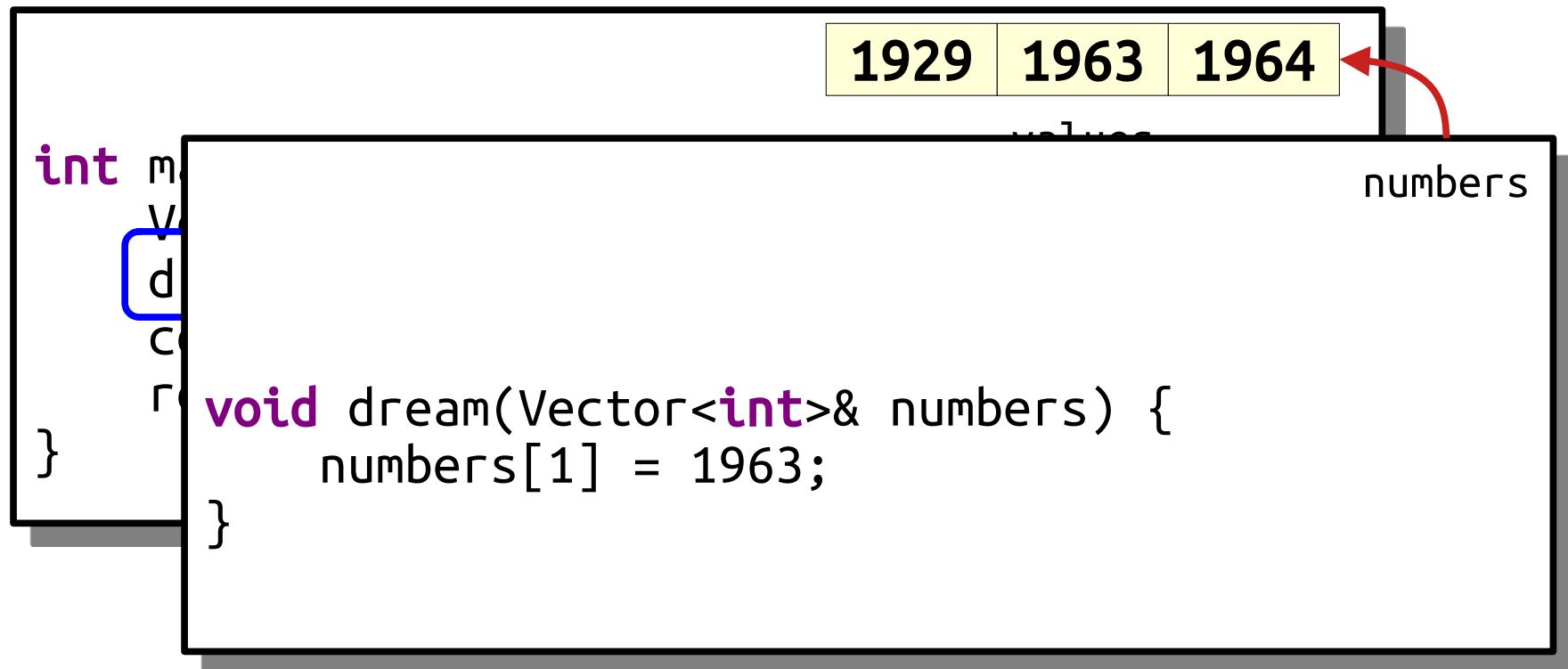
# How it Works Now



# How it Works Now



# How it Works Now



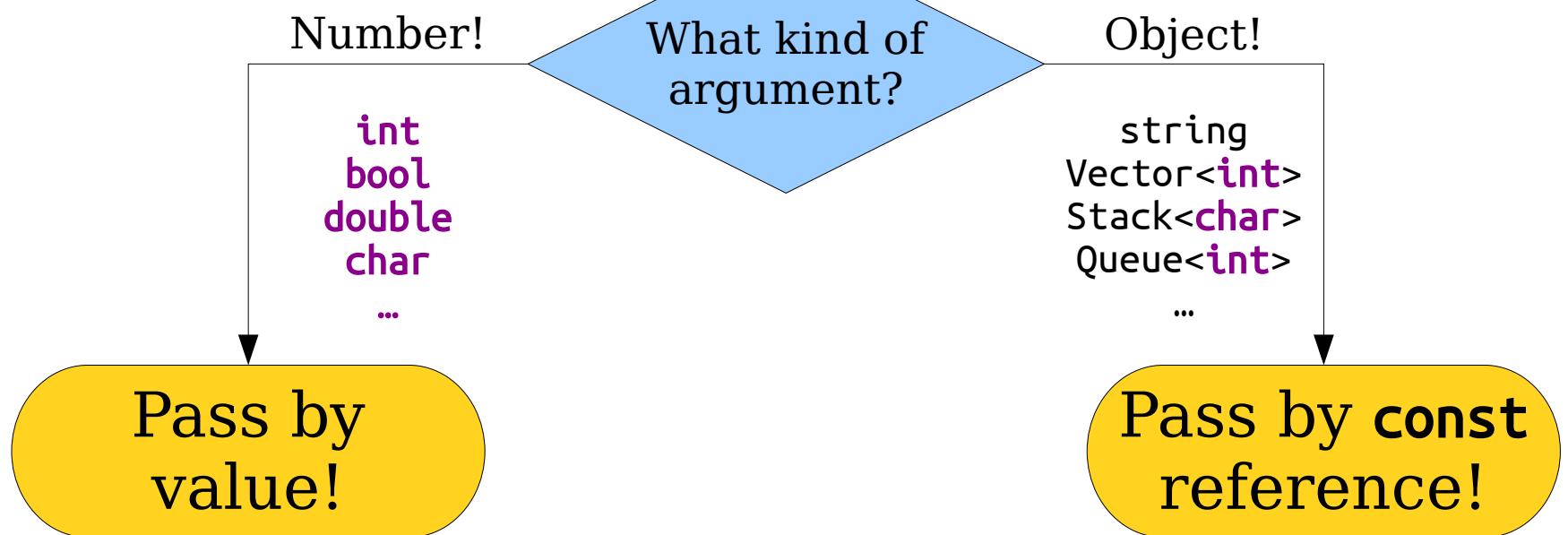
# How it Works Now

```
int main() {  
    Vector<int> values = { 1929, 1955, 1964 };  
    dream(values);  
    cout << values << endl;  
    return 0;  
}
```

1929	1963	1964
------	------	------

values

This is the general convention used in C++ programming. Please feel free to ask questions about this over the course of the quarter!



# Recursion on Vectors

# Finding the Largest Number

# Finding the Largest Number

- Our goal is to write a function

```
int maxOf(const Vector<int>& numbers);
```

that takes as input a `Vector<int>`, then returns the largest number in the `Vector`.

- We're going to assume the `Vector` has at least one element in it; otherwise, it's not possible to return the largest value!
- Let's see how to do this.

# Thinking Recursively

**if** (*The problem is very simple*) {

*Directly solve the problem.*

*Return the solution.*

} **else** {

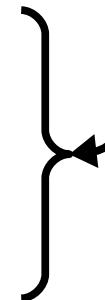
*Split the problem into one or more smaller problems with the same structure as the original.*

*Solve each of those smaller problems.*

*Combine the results to get the overall solution.*

*Return the overall solution.*

}



These simple cases are called *base cases*.



These are the *recursive cases*.

1

2

5

8

1

2

5

8

I B E X

I B E X

elems

137

271

828

182

The largest element of  
this `Vector<int>` is  
either...

... the first  
element of the  
`Vector<int>`, ...

137

elems[0]

... or the largest  
element in this  
`Vector<int>`.

271

828

182

elems.subList(1)

# Tracing the Recursion

```
int main() {
    Vector<int> v = { 2, 7, 1 };
    cout << maxOf(v) << endl;
    return 0;
}
```

# Tracing the Recursion

```
int main() {
    Vector<int> v = { 2, 7, 1 };
    cout << max0T(v) << endl;
    return 0;
}
```

# Tracing the Recursion

```
int main() {
    Vector<int> v = { 2, 7, 1 };
    cout << max0T(v) << endl;
    return 0;
}
```

v 

2	7	1
---	---	---

# Tracing the Recursion

```
int main() {  
    Vector<int> v = { 2, 7, 1 };  
    cout << maxOf(v) << endl;  
    return 0;  
}
```

v 

2	7	1
---	---	---

# Tracing the Recursion

```
int main() {  
    Vector<int> v = { 2, 7, 1 };  
    cout << maxOf(v) << endl;  
    return 0;  
}
```

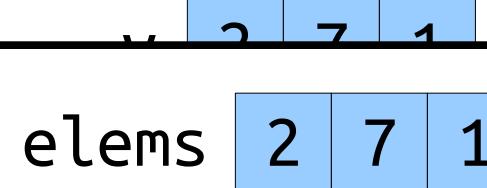
v 

2	7	1
---	---	---

# Tracing the Recursion

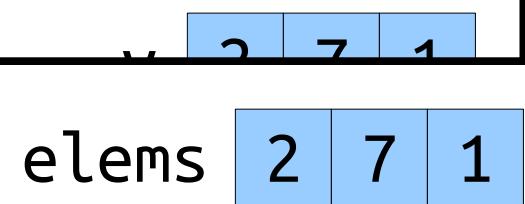
i

```
int maxOf(const Vector<int>& elems) {  
    if (elems.size() == 1) {  
        return elems[0];  
    } else {  
        int first = elems[0];  
        Vector<int> rest = elems.subList(1);  
        return max(first, maxOf(rest));  
    }  
}
```



# Tracing the Recursion

```
i int maxOf(const Vector<int>& elems) {  
    if (elems.size() == 1) {  
        return elems[0];  
    } else {  
        int first = elems[0];  
        Vector<int> rest = elems.subList(1);  
        return max(first, maxOf(rest));  
    }  
}
```



# Tracing the Recursion

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    } else {  
        int first = elems[0];  
        Vector<int> rest = elems.subList(1);  
        return max(first, maxOf(rest));  
    }  
}
```

elems 

... 2 7 1

# Tracing the Recursion

i

```
int maxOf(const Vector<int>& elems) {  
    if (elems.size() == 1) {  
        return elems[0];  
    } else {  
        int first = elems[0];  
        Vector<int> rest = elems.subList(1);  
        return max(first, maxOf(rest));  
    }  
}
```

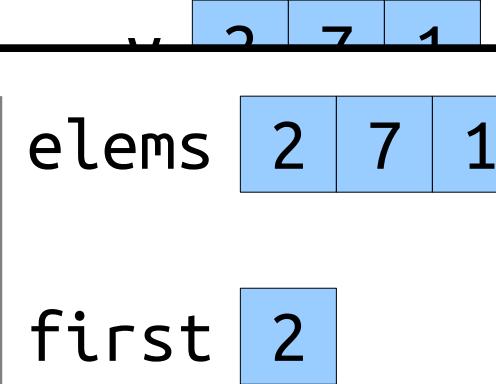
elems 

... 2 7 1

# Tracing the Recursion

i

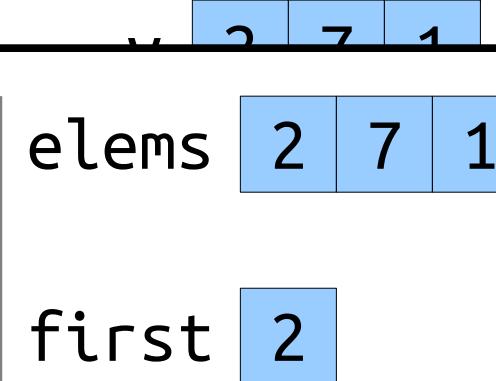
```
int maxOf(const Vector<int>& elems) {  
    if (elems.size() == 1) {  
        return elems[0];  
    } else {  
        int first = elems[0];  
        Vector<int> rest = elems.subList(1);  
        return max(first, maxOf(rest));  
    }  
}
```



# Tracing the Recursion

i

```
int maxOf(const Vector<int>& elems) {  
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        return elems[0];  
    } else {  
        int first = elems[0];  
        Vector<int> rest = elems.subList(1);  
        return max(first, maxOf(rest));  
    }  
}
```



# Tracing the Recursion

i

```
int maxOf(const Vector<int>& elems) {  
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        return elems[0];  
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        int first = elems[0];  
        Vector<int> rest = elems.subList(1);  
        return max(first, maxOf(rest));  
    }  
}
```



# Tracing the Recursion

i

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        Vector<int> rest = elems sublist(1);  
        return max(first, maxOf(rest));  
    }  
}
```



# Tracing the Recursion

i

```
int maxOf(const Vector<int>& elems) {  
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        return elems[0];  
    } else {  
        int first = elems[0];  
        Vector<int> rest = elems.subList(1);  
        return max(first, maxOf(rest));  
    }  
}
```



# Tracing the Recursion

i

```
int maxOf(const Vector<int>& elems) {  
    if (elems.size() == 1) {  
        return elems[0];  
    } else {  
        int first = elems[0];  
        Vector<int> rest = elems.subList(1);  
        return max(first, maxOf(rest));  
    }  
}
```

2



# Tracing the Recursion

i

```
int maxOf(const Vector<int>& elems) {  
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        return elems[0];  
    } else {  
        int first = elems[0];  
        Vector<int> rest = elems sublist(1);  
        return max(first, maxOf(rest));  
    }  
}
```

2

... 2 7 1

elems 2 7 1

first 2

rest 7 1

# Tracing the Recursion

i

```
int maxOf(const Vector<int>& elems) {
```

```
    int maxOf(const Vector<int>& elems) {
        if (elems.size() == 1) {
            return elems[0];
        } else {
            int first = elems[0];
            Vector<int> rest = elems.subList(1);
            return max(first, maxOf(rest));
        }
    }
```



# Tracing the Recursion

i

```
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    } else {  
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        return max(first, maxOf(rest));  
    }  
}
```



# Tracing the Recursion

i

```
int maxOf(const Vector<int>& elems) {
```

```
    int maxOf(const Vector<int>& elems) {
        if (elems.size() == 1) {
            return elems[0];
        } else {
            int first = elems[0];
            Vector<int> rest = elems.subList(1);
            return max(first, maxOf(rest));
        }
    }
```

elems

7 1

elems

2 7 1

elems

2 7 1

# Tracing the Recursion

i

```
int maxOf(const Vector<int>& elems) {
```

```
    int maxOf(const Vector<int>& elems) {
```

```
        if (elems.size() == 1) {
```

```
            return elems[0];
```

```
        } else {
```

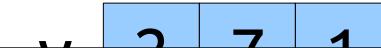
```
            int first = elems[0];
```

```
            Vector<int> rest = elems.subList(1);
```

```
            return max(first, maxOf(rest));
```

```
        }
```

```
}
```



# Tracing the Recursion

i

```
int maxOf(const Vector<int>& elems) {  
    if (elems.size() == 1) {  
        return elems[0];  
    } else {  
        int first = elems[0];  
        vector<int> rest = elems.subList(1);  
        return max(first, maxOf(rest));  
    }  
}
```



# Tracing the Recursion

i

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int maxOf(const Vector<int>& elems) {  
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            return elems[0];  
        } else {  
            int first = elems[0];  
            Vector<int> rest = elems.subList(1);  
            return max(first, maxOf(rest));  
        }  
    }  
}
```



# Tracing the Recursion

i

```
int maxOf(const Vector<int>& elems) {  
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        } else {  
            int first = elems[0];  
            Vector<int> rest = elems.subList(1);  
            return max(first, maxOf(rest));  
        }  
    }  
}
```

elems [2 7 1]

elems [2 7 1]

elems [7 1]

first 7

rest 1

# Tracing the Recursion

i

```
int maxOf(const Vector<int>& elems) {  
    int maxOf(const Vector<int>& elems) {  
        if (elems.size() == 1) {  
            return elems[0];  
        } else {  
            int first = elems[0];  
            Vector<int> rest = elems sublist(1);  
            return max(first, maxOf(rest));  
        }  
    }  
}
```

elems 2 7 1

elems 2 7 1

elems 7 1

first 7

rest 1

# Tracing the Recursion

i

```
int maxOf(const Vector<int>& elems) {  
    int maxOf(const Vector<int>& elems) {  
        if (elems.size() == 1) {  
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        } else {  
            int first = elems[0];  
            Vector<int> rest = elems.subList(1);  
            return max(first, maxOf(rest));  
        }  
    }  
}
```

elems 2 7 1

elems 2 7 1

elems 7 1

first 7

rest 1

# Tracing the Recursion

i

```
int maxOf(const Vector<int>& elems) {  
    int maxOf(const Vector<int>& elems) {  
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        } else {  
            int first = elems[0];  
            Vector<int> rest = elems.subList(1);  
            return max(first, maxOf(rest));  
        }  
    }  
}
```

7

elems 2 7 1

elems 2 7 1

elems 7 1

first 7

rest 1

# Tracing the Recursion

i

```
int maxOf(const Vector<int>& elems) {  
    int maxOf(const Vector<int>& elems) {  
        if (elems.size() == 1) {  
            return elems[0];  
        } else {  
            int first = elems[0];  
            Vector<int> rest = elems sublist(1);  
            return max(first, maxOf(rest));  
        }  
    }  
}
```

7

elems 2 7 1

elems 2 7 1

elems 7 1

first 7

rest 1

# Tracing the Recursion

i

```
int maxOf(const Vector<int>& elems) {
```

```
    int maxOf(const Vector<int>& elems) {
```

}

```
        int maxOf(const Vector<int>& elems) {
```

```
            if (elems.size() == 1) {
```

```
                return elems[0];
```

```
            } else {
```

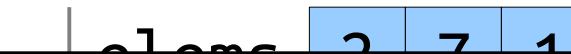
```
                int first = elems[0];
```

```
                Vector<int> rest = elems.subList(1);
```

```
                return max(first, maxOf(rest));
```

```
            }
```

```
        }
```



elems 1

# Tracing the Recursion

```
i int maxOf(const Vector<int>& elems) {  
    int maxOf(const Vector<int>& elems) {  
        }  
        int maxOf(const Vector<int>& elems) {  
            if (elems.size() == 1) {  
                return elems[0];  
            } else {  
                int first = elems[0];  
                Vector<int> rest = elems.subList(1);  
                return max(first, maxOf(rest));  
            }  
        }  
    }  
}
```

The diagram illustrates the state of the 'elems' vector at different stages of the recursion:

- Initial call: elems = [2, 7, 1]
- First recursive call: elems = [7, 1]
- Second recursive call: elems = [1]

# Tracing the Recursion

i

```
int maxOf(const Vector<int>& elems) {
```

```
    int maxOf(const Vector<int>& elems) {
```

}

```
        int maxOf(const Vector<int>& elems) {
```

```
            if (elems.size() == 1) {
```

```
                return elems[0];
```

```
            } else {
```

```
                int first = elems[0];
```

```
                Vector<int> rest = elems.subList(1);
```

```
                return max(first, maxOf(rest));
```

```
            }
```

```
        }
```



elems 1

# Tracing the Recursion

i

```
int maxOf(const Vector<int>& elems) {
```

```
    int maxOf(const Vector<int>& elems) {
```

}

```
        int maxOf(const Vector<int>& elems) {
```

```
            if (elems.size() == 1) {
```

```
                return elems[0];
```

```
            } else {
```

```
                int first = elems[0];
```

```
                Vector<int> rest = elems.subList(1);
```

```
                return max(first, maxOf(rest));
```

```
            }
```

```
        }
```



elems 1

# Tracing the Recursion

i

```
int maxOf(const Vector<int>& elems) {
```

```
    int maxOf(const Vector<int>& elems) {
```

}

```
        int maxOf(const Vector<int>& elems) {
```

```
            if (elems.size() == 1) {
```

```
                return elems[0];
```

1

```
            } else {
```

```
                int first = elems[0];
```

```
                Vector<int> rest = elems.subList(1);
```

```
                return max(first, maxOf(rest));
```

}

```
}
```

```
}
```



elems 1

# Tracing the Recursion

i

```
int maxOf(const Vector<int>& elems) {  
    int maxOf(const Vector<int>& elems) {  
        if (elems.size() == 1) {  
            return elems[0];  
        } else {  
            int first = elems[0];  
            Vector<int> rest = elems sublist(1);  
            return max(first, maxOf(rest));  
        }  
    }  
}
```

7      1

elems 2 7 1

elems 2 7 1

elems 7 1

first 7

rest 1

# Tracing the Recursion

i

```
int maxOf(const Vector<int>& elems) {  
    int maxOf(const Vector<int>& elems) {  
        if (elems.size() == 1) {  
            return elems[0];  
        } else {  
            int first = elems[0];  
            Vector<int> rest = elems sublist(1);  
            return max(first, maxOf(rest));  
        }  
    }  
}
```

7      1

elems 2 7 1

elems 2 7 1

elems 7 1

first 7

rest 1

# Tracing the Recursion

i

```
int maxOf(const Vector<int>& elems) {  
    int maxOf(const Vector<int>& elems) {  
        if (elems.size() == 1) {  
            return elems[0];  
        } else {  
            int first = elems[0];  
            Vector<int> rest = elems sublist(1);  
            return max(first, maxOf(rest));  
        }  
    }  
}
```

7

elems 2 7 1

elems 2 7 1

elems 7 1

first 7

rest 1

# Tracing the Recursion

i

```
int maxOf(const Vector<int>& elems) {  
    int maxOf(const Vector<int>& elems) {  
        if (elems.size() == 1) {  
            return elems[0];  
        } else {  
            int first = elems[0];  
            Vector<int> rest = elems sublist(1);  
            return max(first, maxOf(rest));  
        }  
    }  
}
```

7

elems 2 7 1

elems 2 7 1

elems 7 1

first 7

rest 1

# Tracing the Recursion

i

```
int maxOf(const Vector<int>& elems) {  
    if (elems.size() == 1) {  
        return elems[0];  
    } else {  
        int first = elems[0];  
        Vector<int> rest = elems sublist(1);  
        return max(first, maxOf(rest));  
    }  
}
```

2            7

... 2 7 1

elems 2 7 1

first 2

rest 7 1

# Tracing the Recursion

i

```
int maxOf(const Vector<int>& elems) {  
    if (elems.size() == 1) {  
        return elems[0];  
    } else {  
        int first = elems[0];  
        Vector<int> rest = elems sublist(1);  
        return max(first, maxOf(rest));  
    }  
}
```

2                    7

... 2 7 1

elems 2 7 1

first 2

rest 7 1

# Tracing the Recursion

i

```
int maxOf(const Vector<int>& elems) {  
    if (elems.size() == 1) {  
        return elems[0];  
    } else {  
        int first = elems[0];  
        Vector<int> rest = elems sublist(1);  
        return max(first, maxOf(rest));  
    }  
}
```

7



# Tracing the Recursion

i

```
int maxOf(const Vector<int>& elems) {  
    if (elems.size() == 1) {  
        return elems[0];  
    } else {  
        int first = elems[0];  
        Vector<int> rest = elems sublist(1);  
        return max(first, maxOf(rest));  
    }  
}
```

7



# Tracing the Recursion

```
int main() {  
    Vector<int> v = { 2, 7, 1 };  
    cout << maxOf(v) << endl;  
    return 0;    7  
}
```

v 

2	7	1
---	---	---

# Summary from Today

- The `Vector<T>` type in C++ represents a sequence of elements.
- Parameters in C++ are passed by *value* by default. You can change that to use pass by *reference* if you'd like.
- Use pass-by-**const**-reference for objects you don't intend to change.
- Each stack frame from a recursive function gets its own copies of all the local variables.

# Your Action Items

- ***Read Chapter 5.1 and Chapter 5.2 of the textbook.***
  - It's all about Vector and Grid! There are some goodies there.
- ***Work on Assignment 1.***
  - Aim to complete the Debugger Warmups and Fire by Monday and to start Only Connect on Monday.
- ***Explore the maxOf example.***
  - Tinker and play around with this one. See if you can get very comfortable with how it works.

# Next Time

- *Lexicons, Sets, and Maps.*
  - Storing words.
  - Storing items in No Particular Order.
  - Associating items with one another.

**Appendix:** Finding the max, another way.

elems

137	271	828	182
-----	-----	-----	-----

The largest element of  
this `Vector<int>` is  
either...

... the largest  
element in this  
`Vector<int>`, ...

137	271
-----	-----

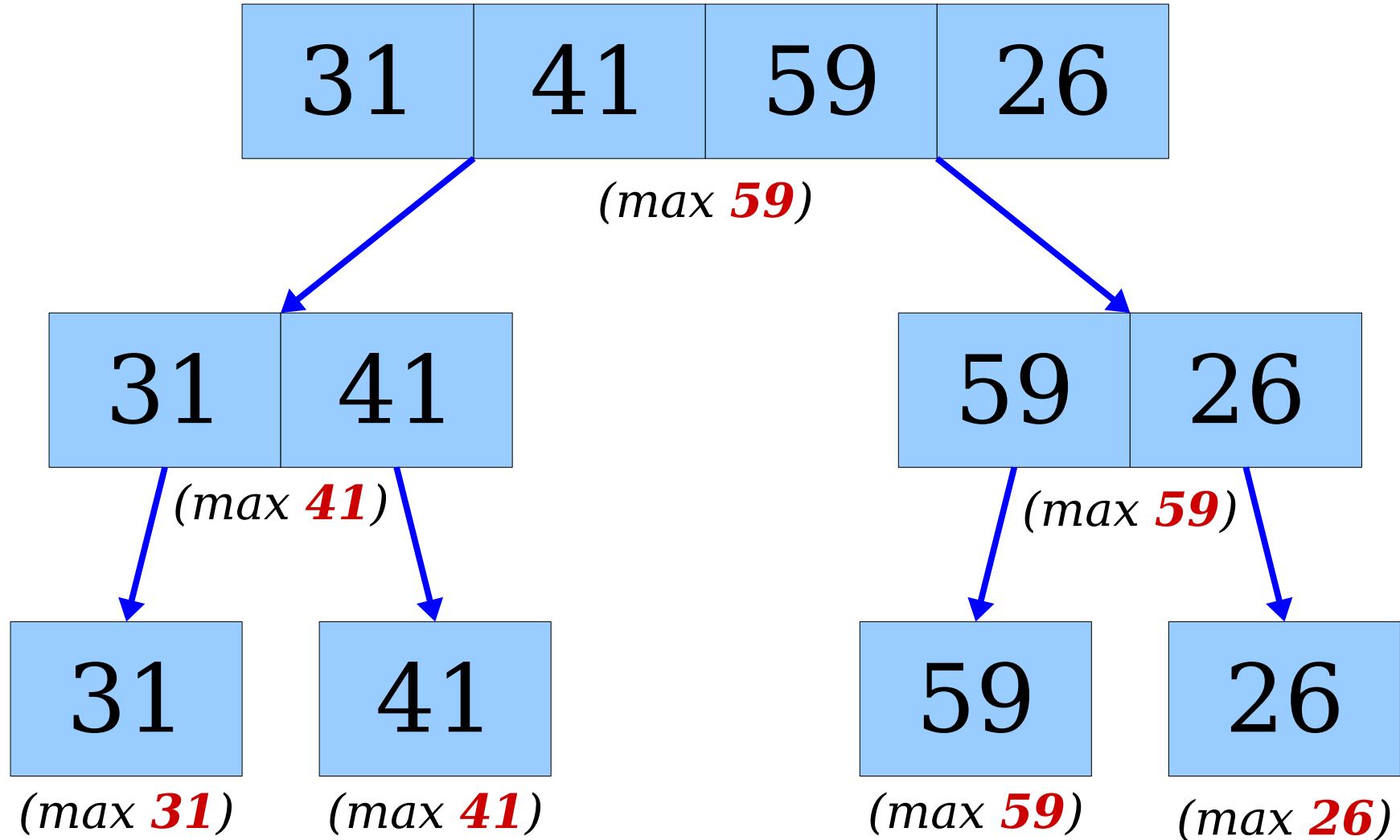
... or the largest  
element in this  
`Vector<int>`.

828	182
-----	-----

`elems.subList(0, elems.size() / 2)`

`elems.subList(elems.size() / 2)`

# max0f as a Tournament



# maxOf as a Tournament

```
int maxOf(const Vector<int>& elems) {
    if (elems.size() == 1) {
        return elems[0];
    } else {
        int half = elems.size() / 2;

        /* First half of the elements. */
        Vector<int> left = elems.subList(0, half);

        /* Second half of the elements. */
        Vector<int> right = elems.subList(half);

        /* Biggest value in the overall list is either
         * the largest element in the first half or
         * the largest element in the second half.
         */
        return max(maxOf(left), maxOf(right));
    }
}
```

# Tracing the Recursion

```
int main() {
    Vector<int> v = { 31, 41, 59, 26 };
    cout << maxOf(v) << endl;
    return 0;
}
```

# Tracing the Recursion

```
int main() {
    Vector<int> v = { 31, 41, 59, 26 };
    cout << maxOf(v) << endl;
    return 0;
}
```

# Tracing the Recursion

v 31 41 59 26

```
int main() {  
    Vector<int> v = { 31, 41, 59, 26 };  
    cout << maxOf(v) << endl;  
    return 0;  
}
```

# Tracing the Recursion

v 31 41 59 26

```
int main() {  
    Vector<int> v = { 31, 41, 59, 26 };  
    cout << maxOf(v) << endl;  
    return 0;  
}
```

# Tracing the Recursion

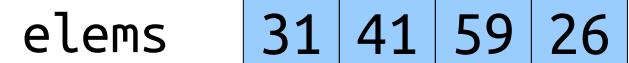
v 31 41 59 26

```
int main() {  
    Vector<int> v = { 31, 41, 59, 26 };  
    cout << maxOf(v) << endl;  
    return 0;  
}
```

# Tracing the Recursion

i

```
int maxOf(const Vector<int>& elems) {  
    if (elems.size() == 1) {  
        return elems[0];  
    } else {  
        int half = elems.size() / 2;  
        Vector<int> left = elems.subList(0, half);  
        Vector<int> right = elems.subList(half);  
        return max(maxOf(left), maxOf(right));  
    }  
}
```



# Tracing the Recursion

i

```
int maxOf(const Vector<int>& elems) {
    if (elems.size() == 1) {
        return elems[0];
    } else {
        int half = elems.size() / 2;
        Vector<int> left = elems.subList(0, half);
        Vector<int> right = elems.subList(half);
        return max(maxOf(left), maxOf(right));
    }
}
```

v 31 41 59 26

elems 31 41 59 26

# Tracing the Recursion

i

```
int maxOf(const Vector<int>& elems) {  
    if (elems.size() == 1) {  
        return elems[0];  
    } else {  
        int half = elems.size() / 2;  
        Vector<int> left = elems.subList(0, half);  
        Vector<int> right = elems.subList(half);  
        return max(maxOf(left), maxOf(right));  
    }  
}
```



# Tracing the Recursion

i

```
int maxOf(const Vector<int>& elems) {  
    if (elems.size() == 1) {  
        return elems[0];  
    } else {  
        int half = elems.size() / 2;  
        Vector<int> left = elems.subList(0, half);  
        Vector<int> right = elems.subList(half);  
        return max(maxOf(left), maxOf(right));  
    }  
}
```



# Tracing the Recursion

i

```
int maxOf(const Vector<int>& elems) {  
    if (elems.size() == 1) {  
        return elems[0];  
    } else {  
        int half = elems.size() / 2;  
        Vector<int> left = elems.subList(0, half);  
        Vector<int> right = elems.subList(half);  
        return max(maxOf(left), maxOf(right));  
    }  
}
```

v 31 41 59 26

elems	31	41	59	26
half	2			

# Tracing the Recursion

i

```
int maxOf(const Vector<int>& elems) {  
    if (elems.size() == 1) {  
        return elems[0];  
    } else {  
        int half = elems.size() / 2;  
        Vector<int> left  = elems.subList(0, half);  
        vector<int> right = elems.SUBLIS(half);  
        return max(maxOf(left), maxOf(right));  
    }  
}
```

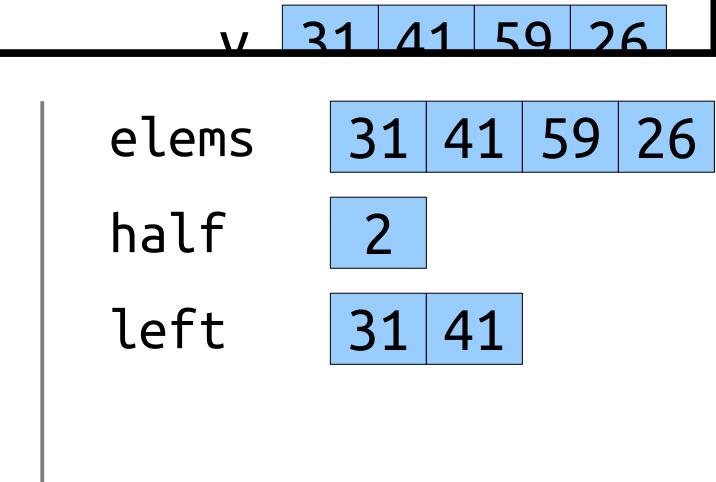
v 31 41 59 26

elems	31	41	59	26
half	2			

# Tracing the Recursion

i

```
int maxOf(const Vector<int>& elems) {  
    if (elems.size() == 1) {  
        return elems[0];  
    } else {  
        int half = elems.size() / 2;  
        Vector<int> left = elems.subList(0, half);  
        vector<int> right = elems.SUBLIS(half);  
        return max(maxOf(left), maxOf(right));  
    }  
}
```



# Tracing the Recursion

i

```
int maxOf(const Vector<int>& elems) {  
    if (elems.size() == 1) {  
        return elems[0];  
    } else {  
        int half = elems.size() / 2;  
        Vector<int> left = elems.subList(0, half);  
        Vector<int> right = elems.subList(half);  
        return max(maxOf(left), maxOf(right));  
    }  
}
```

v 31 41 59 26

elems	31	41	59	26
half	2			
left	31	41		

# Tracing the Recursion

i

```
int maxOf(const Vector<int>& elems) {  
    if (elems.size() == 1) {  
        return elems[0];  
    } else {  
        int half = elems.size() / 2;  
        Vector<int> left = elems.subList(0, half);  
        Vector<int> right = elems.subList(half);  
        return max(maxOf(left), maxOf(right));  
    }  
}
```

v 31 41 59 26

elems	31 41 59 26
half	2
left	31 41
right	59 26

# Tracing the Recursion

i

```
int maxOf(const Vector<int>& elems) {  
    if (elems.size() == 1) {  
        return elems[0];  
    } else {  
        int half = elems.size() / 2;  
        Vector<int> left = elems.subList(0, half);  
        Vector<int> right = elems.subList(half);  
        return max(maxOf(left), maxOf(right));  
    }  
}
```



elems	31	41	59	26
half	2			
left	31	41		
right	59	26		

# Tracing the Recursion

i

```
int maxOf(const Vector<int>& elems) {  
    if (elems.size() == 1) {  
        return elems[0];  
    } else {  
        int half = elems.size() / 2;  
        Vector<int> left = elems.subList(0, half);  
        Vector<int> right = elems.subList(half);  
        return max(maxOf(left), maxOf(right));  
    }  
}
```

v 31 41 59 26

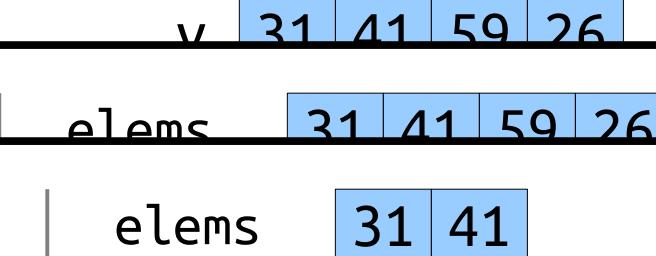
elems	31	41	59	26
half	2			
left	31	41		
right	59	26		

# Tracing the Recursion

i

i

```
int maxOf(const Vector<int>& elems) {  
    if (elems.size() == 1) {  
        return elems[0];  
    } else {  
        int half = elems.size() / 2;  
        Vector<int> left  = elems.subList(0, half);  
        Vector<int> right = elems.subList(half);  
        return max(maxOf(left), maxOf(right));  
    }  
}
```



# Tracing the Recursion

i  
i

```
int maxOf(const Vector<int>& elems) {  
    if (elems.size() == 1) {  
        return elems[0];  
    } else {  
        int half = elems.size() / 2;  
        Vector<int> left  = elems.subList(0, half);  
        Vector<int> right = elems.subList(half);  
        return max(maxOf(left), maxOf(right));  
    }  
}
```



# Tracing the Recursion

i  
i

```
int maxOf(const Vector<int>& elems) {  
    if (elems.size() == 1) {  
        return elems[0];  
    } else {  
        int half = elems.size() / 2;  
        Vector<int> left = elems.subList(0, half);  
        Vector<int> right = elems.subList(half);  
        return max(maxOf(left), maxOf(right));  
    }  
}
```

v 31 41 59 26

elems 31 41 59 26

elems 31 41

# Tracing the Recursion

i  
i

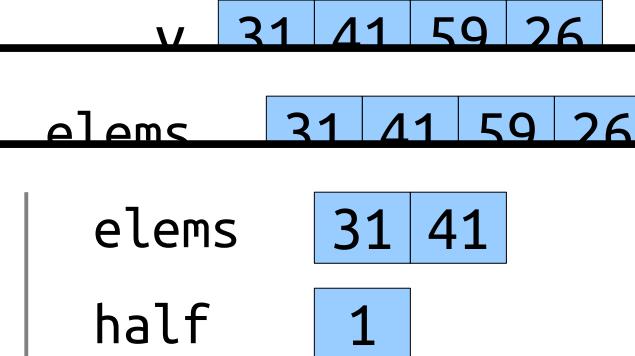
```
int maxOf(const Vector<int>& elems) {  
    if (elems.size() == 1) {  
        return elems[0];  
    } else {  
        int half = elems.size() / 2;  
        vector<int> left = elems.subList(0, half);  
        Vector<int> right = elems.subList(half);  
        return max(maxOf(left), maxOf(right));  
    }  
}
```



# Tracing the Recursion

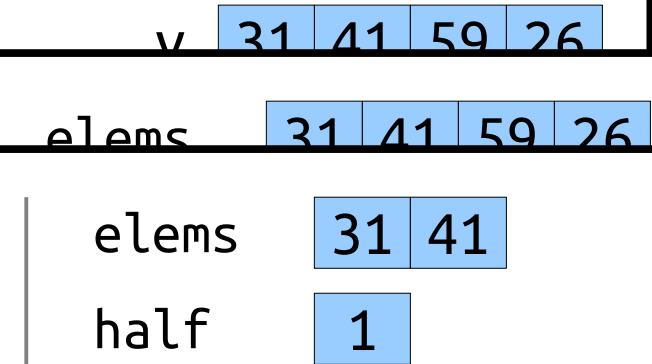
i  
i

```
int maxOf(const Vector<int>& elems) {  
    if (elems.size() == 1) {  
        return elems[0];  
    } else {  
        int half = elems.size() / 2;  
        vector<int> left = elems.subList(0, half);  
        Vector<int> right = elems.subList(half);  
        return max(maxOf(left), maxOf(right));  
    }  
}
```



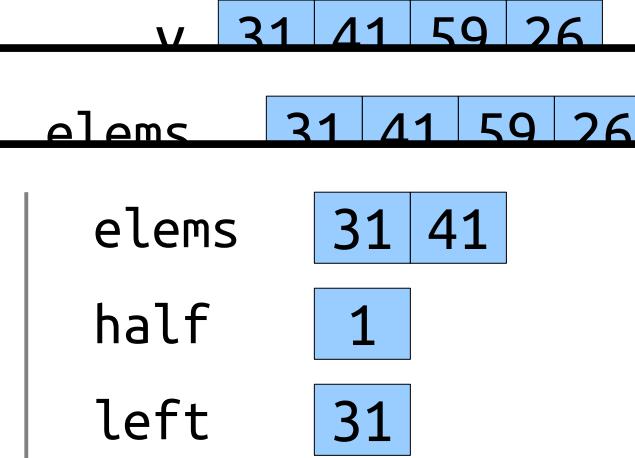
# Tracing the Recursion

```
i i  
int maxOf(const Vector<int>& elems) {  
    if (elems.size() == 1) {  
        return elems[0];  
    } else {  
        int half = elems.size() / 2;  
        Vector<int> left  = elems.subList(0, half);  
        vector<int> right = elems.subList(half);  
        return max(maxOf(left), maxOf(right));  
    }  
}
```



# Tracing the Recursion

```
i i  
int maxOf(const Vector<int>& elems) {  
    if (elems.size() == 1) {  
        return elems[0];  
    } else {  
        int half = elems.size() / 2;  
        Vector<int> left  = elems.subList(0, half);  
        vector<int> right = elems.subList(half);  
        return max(maxOf(left), maxOf(right));  
    }  
}
```



# Tracing the Recursion

i

```
int maxOf(const Vector<int>& elems) {  
    if (elems.size() == 1) {  
        return elems[0];  
    } else {  
        int half = elems.size() / 2;  
        Vector<int> left = elems.subList(0, half);  
        Vector<int> right = elems.subList(half);  
        return max(maxOf(left), maxOf(right));  
    }  
}
```

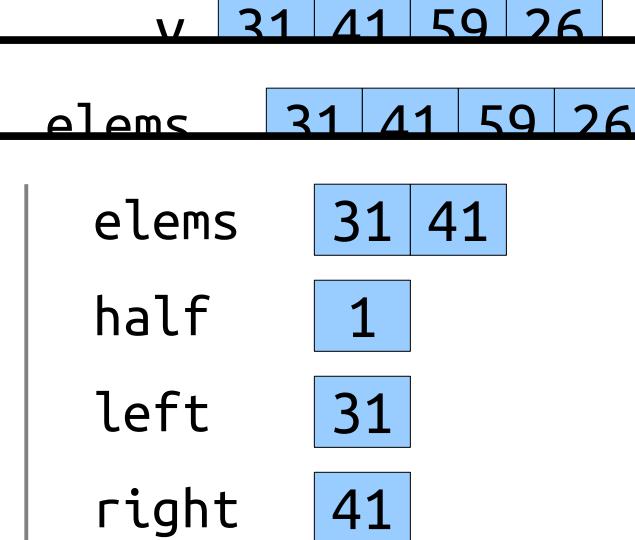


# Tracing the Recursion

i

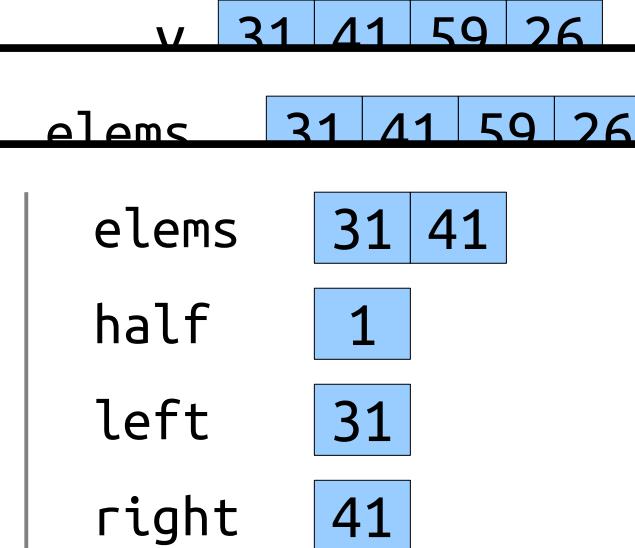
i

```
int maxOf(const Vector<int>& elems) {  
    if (elems.size() == 1) {  
        return elems[0];  
    } else {  
        int half = elems.size() / 2;  
        Vector<int> left = elems.subList(0, half);  
        Vector<int> right = elems.subList(half);  
        return max(maxOf(left), maxOf(right));  
    }  
}
```



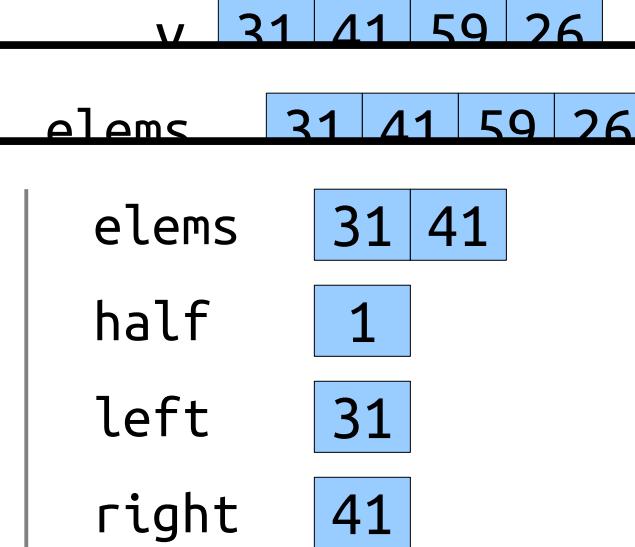
# Tracing the Recursion

```
i i  
int maxOf(const Vector<int>& elems) {  
    if (elems.size() == 1) {  
        return elems[0];  
    } else {  
        int half = elems.size() / 2;  
        Vector<int> left  = elems.subList(0, half);  
        Vector<int> right = elems.subList(half);  
        return max(maxOf(left), maxOf(right));  
    }  
}
```



# Tracing the Recursion

```
i i  
int maxOf(const Vector<int>& elems) {  
    if (elems.size() == 1) {  
        return elems[0];  
    } else {  
        int half = elems.size() / 2;  
        Vector<int> left  = elems.subList(0, half);  
        Vector<int> right = elems.subList(half);  
        return max(maxOf(left), maxOf(right));  
    }  
}
```



# Tracing the Recursion

```
int maxOf(const Vector<int>& elems) {
    if (elems.size() == 1) {
        return elems[0];
    } else {
        int half = elems.size() / 2;
        Vector<int> left  = elems.subList(0, half);
        Vector<int> right = elems.subList(half);
        return max(maxOf(left), maxOf(right));
    }
}
```



# Tracing the Recursion

```
int maxOf(const Vector<int>& elems) {  
    if (elems.size() == 1) {  
        return elems[0];  
    } else {  
        int half = elems.size() / 2;  
        Vector<int> left  = elems.subList(0, half);  
        Vector<int> right = elems.subList(half);  
        return max(maxOf(left), maxOf(right));  
    }  
}
```



# Tracing the Recursion

```
int maxOf(const Vector<int>& elems) {
    if (elems.size() == 1) {
        return elems[0];
    } else {
        int half = elems.size() / 2;
        Vector<int> left = elems.subList(0, half);
        Vector<int> right = elems.subList(half);
        return max(maxOf(left), maxOf(right));
    }
}
```



# Tracing the Recursion

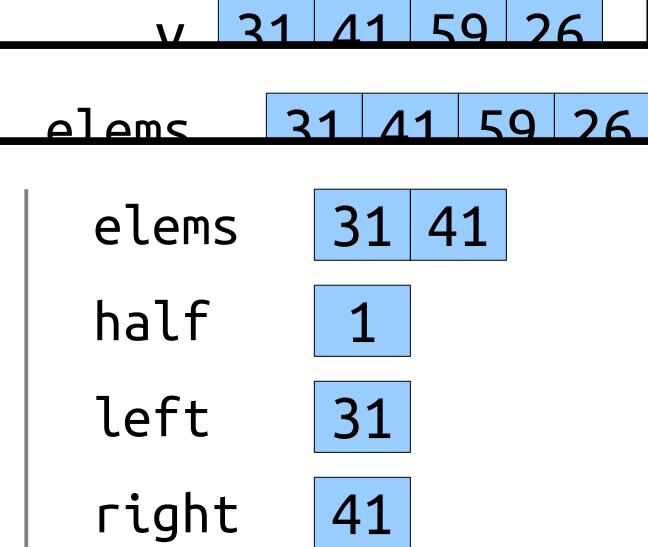
```
int maxOf(const Vector<int>& elems) {
    if (elems.size() == 1) {
        return elems[0]; 31
    } else {
        int half = elems.size() / 2;
        Vector<int> left = elems.subList(0, half);
        Vector<int> right = elems.subList(half);
        return max(maxOf(left), maxOf(right));
    }
}
```



# Tracing the Recursion

```
i i  
int maxOf(const Vector<int>& elems) {  
    if (elems.size() == 1) {  
        return elems[0];  
    } else {  
        int half = elems.size() / 2;  
        Vector<int> left  = elems.subList(0, half);  
        Vector<int> right = elems.subList(half);  
        return max(maxOf(left), maxOf(right));  
    }  
}
```

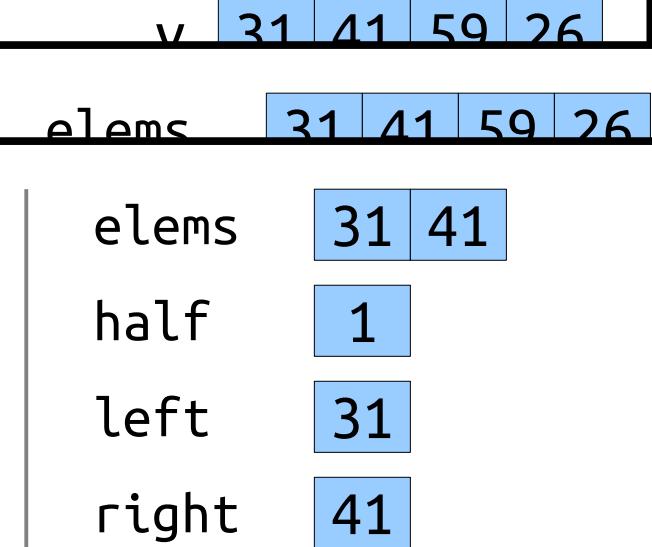
31



# Tracing the Recursion

```
i i  
int maxOf(const Vector<int>& elems) {  
    if (elems.size() == 1) {  
        return elems[0];  
    } else {  
        int half = elems.size() / 2;  
        Vector<int> left = elems.subList(0, half);  
        Vector<int> right = elems.subList(half);  
        return max(maxOf(left), maxOf(right));  
    }  
}
```

31



# Tracing the Recursion

```
int maxOf(const Vector<int>& elems) {
    if (elems.size() == 1) {
        return elems[0];
    } else {
        int half = elems.size() / 2;
        Vector<int> left  = elems.subList(0, half);
        Vector<int> right = elems.subList(half);
        return max(maxOf(left), maxOf(right));
    }
}
```



# Tracing the Recursion

```
int maxOf(const Vector<int>& elems) {
    if (elems.size() == 1) {
        return elems[0];
    } else {
        int half = elems.size() / 2;
        Vector<int> left  = elems.subList(0, half);
        Vector<int> right = elems.subList(half);
        return max(maxOf(left), maxOf(right));
    }
}
```



# Tracing the Recursion

```
int maxOf(const Vector<int>& elems) {
    if (elems.size() == 1) {
        return elems[0];
    } else {
        int half = elems.size() / 2;
        Vector<int> left = elems.subList(0, half);
        Vector<int> right = elems.subList(half);
        return max(maxOf(left), maxOf(right));
    }
}
```



# Tracing the Recursion

```
int maxOf(const Vector<int>& elems) {
    if (elems.size() == 1) {
        return elems[0]; 41
    } else {
        int half = elems.size() / 2;
        Vector<int> left = elems.subList(0, half);
        Vector<int> right = elems.subList(half);
        return max(maxOf(left), maxOf(right));
    }
}
```



# Tracing the Recursion

i

i

```
int maxOf(const Vector<int>& elems) {  
    if (elems.size() == 1) {  
        return elems[0];  
    } else {  
        int half = elems.size() / 2;  
        Vector<int> left = elems.subList(0, half);  
        Vector<int> right = elems.subList(half);  
        return max(maxOf(left), maxOf(right));  
    }  
}
```

31

41

v 31 41 59 26

elems 31 41 59 26

elems 31 41

1

left 31

41

# Tracing the Recursion

i

i

```
int maxOf(const Vector<int>& elems) {  
    if (elems.size() == 1) {  
        return elems[0];  
    } else {  
        int half = elems.size() / 2;  
        Vector<int> left  = elems.subList(0, half);  
        Vector<int> right = elems.subList(half);  
        return max(maxOf(left), maxOf(right));  
    }  
}
```

31

41

v 31 41 59 26

elems 31 41 59 26

elems 31 41

half 1

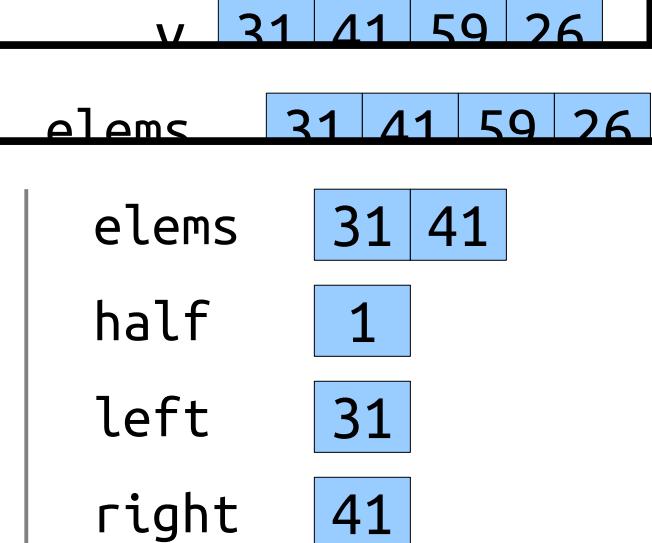
left 31

right 41

# Tracing the Recursion

```
i i  
int maxOf(const Vector<int>& elems) {  
    if (elems.size() == 1) {  
        return elems[0];  
    } else {  
        int half = elems.size() / 2;  
        Vector<int> left  = elems.subList(0, half);  
        Vector<int> right = elems.subList(half);  
        return max(maxOf(left), maxOf(right));  
    }  
}
```

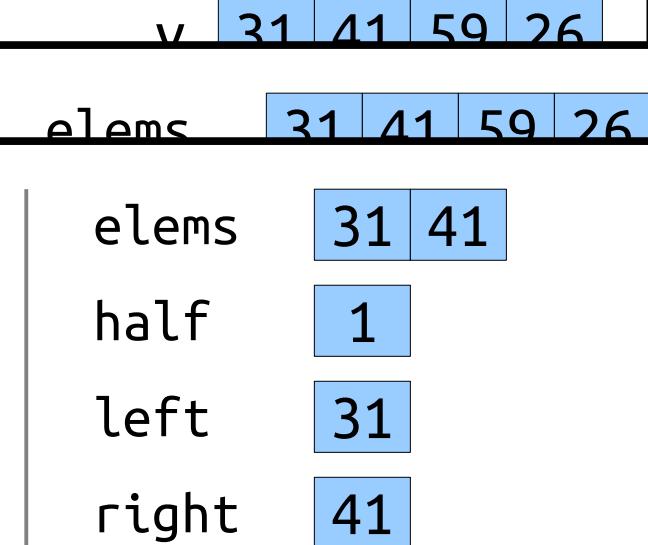
41



# Tracing the Recursion

```
i i  
int maxOf(const Vector<int>& elems) {  
    if (elems.size() == 1) {  
        return elems[0];  
    } else {  
        int half = elems.size() / 2;  
        Vector<int> left  = elems.subList(0, half);  
        Vector<int> right = elems.subList(half);  
        return max(maxOf(left), maxOf(right));  
    }  
}
```

41



# Tracing the Recursion

i

```
int maxOf(const Vector<int>& elems) {  
    if (elems.size() == 1) {  
        return elems[0];  
    } else {  
        int half = elems.size() / 2;  
        Vector<int> left = elems.subList(0, half);  
        Vector<int> right = elems.subList(half);  
        return max(maxOf(left), maxOf(right));  
    }  
}
```

41

v 31 41 59 26

elems	31	41	59	26
half	2			
left	31	41		
right	59	26		

# Tracing the Recursion

i

```
int maxOf(const Vector<int>& elems) {  
    if (elems.size() == 1) {  
        return elems[0];  
    } else {  
        int half = elems.size() / 2;  
        Vector<int> left = elems.subList(0, half);  
        Vector<int> right = elems.subList(half);  
        return max(maxOf(left), maxOf(right));  
    }  
}
```

41

v 31 41 59 26

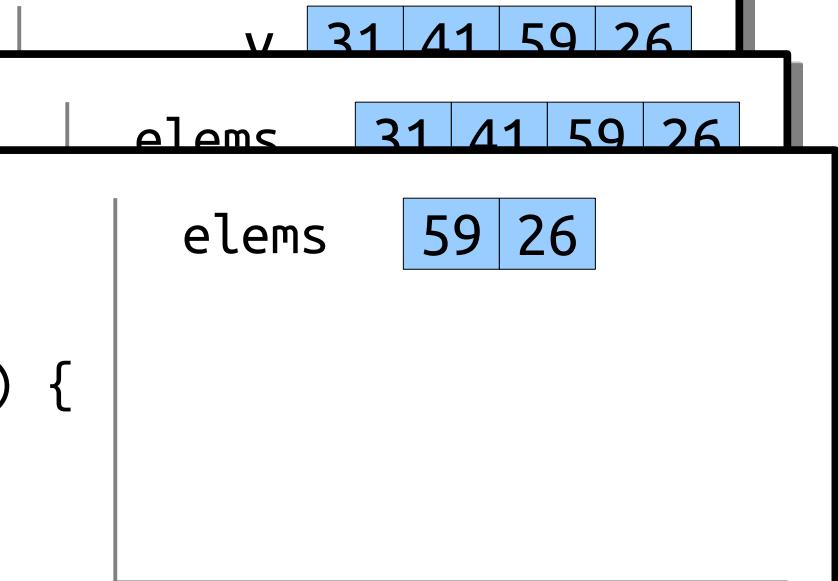
elems	31	41	59	26
half	2			
left	31	41		
right	59	26		

# Tracing the Recursion

i

i

```
int maxOf(const Vector<int>& elems) {  
    if (elems.size() == 1) {  
        return elems[0];  
    } else {  
        int half = elems.size() / 2;  
        Vector<int> left  = elems.subList(0, half);  
        Vector<int> right = elems.subList(half);  
        return max(maxOf(left), maxOf(right));  
    }  
}
```



# Tracing the Recursion

```
int maxOf(const Vector<int>& elems) {
    if (elems.size() == 1) {
        return elems[0];
    } else {
        int half = elems.size() / 2;
        Vector<int> left  = elems.subList(0, half);
        Vector<int> right = elems.subList(half);
        return max(maxOf(left), maxOf(right));
    }
}
```



# Tracing the Recursion

i  
i

```
int maxOf(const Vector<int>& elems) {  
    if (elems.size() == 1) {  
        return elems[0];  
    } else {  
        int half = elems.size() / 2;  
        Vector<int> left = elems.subList(0, half);  
        Vector<int> right = elems.subList(half);  
        return max(maxOf(left), maxOf(right));  
    }  
}
```



# Tracing the Recursion

i  
i

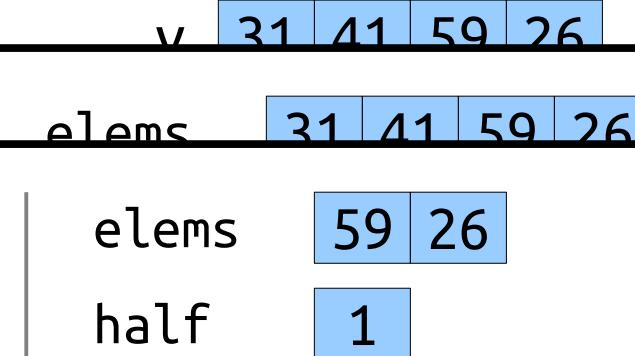
```
int maxOf(const Vector<int>& elems) {  
    if (elems.size() == 1) {  
        return elems[0];  
    } else {  
        int half = elems.size() / 2;  
        vector<int> left = elems.subList(0, half);  
        Vector<int> right = elems.subList(half);  
        return max(maxOf(left), maxOf(right));  
    }  
}
```



# Tracing the Recursion

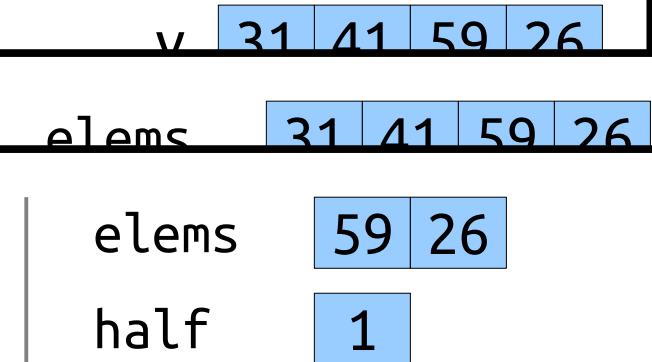
i  
i

```
int maxOf(const Vector<int>& elems) {  
    if (elems.size() == 1) {  
        return elems[0];  
    } else {  
        int half = elems.size() / 2;  
        vector<int> left = elems.subList(0, half);  
        Vector<int> right = elems.subList(half);  
        return max(maxOf(left), maxOf(right));  
    }  
}
```



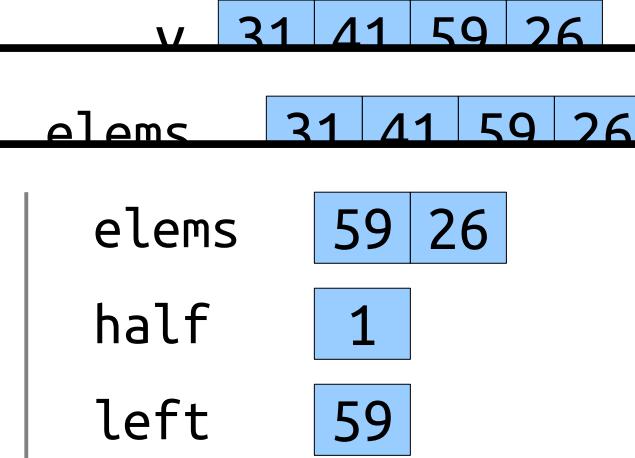
# Tracing the Recursion

```
i i  
int maxOf(const Vector<int>& elems) {  
    if (elems.size() == 1) {  
        return elems[0];  
    } else {  
        int half = elems.size() / 2;  
        Vector<int> left  = elems.subList(0, half);  
        vector<int> right = elems.subList(half);  
        return max(maxOf(left), maxOf(right));  
    }  
}
```



# Tracing the Recursion

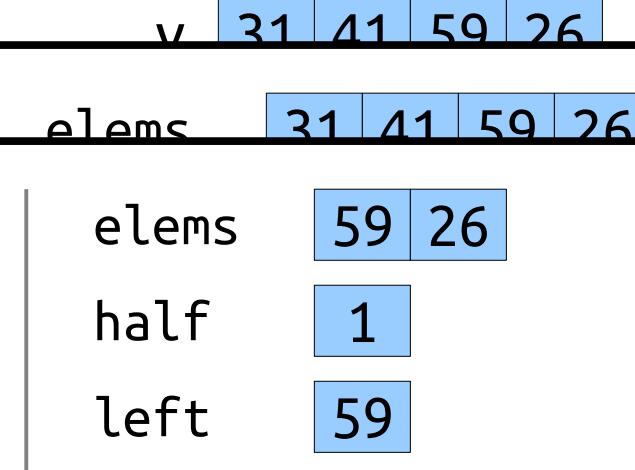
```
i i  
int maxOf(const Vector<int>& elems) {  
    if (elems.size() == 1) {  
        return elems[0];  
    } else {  
        int half = elems.size() / 2;  
        Vector<int> left  = elems.subList(0, half);  
        vector<int> right = elems.subList(half);  
        return max(maxOf(left), maxOf(right));  
    }  
}
```



# Tracing the Recursion

i  
i

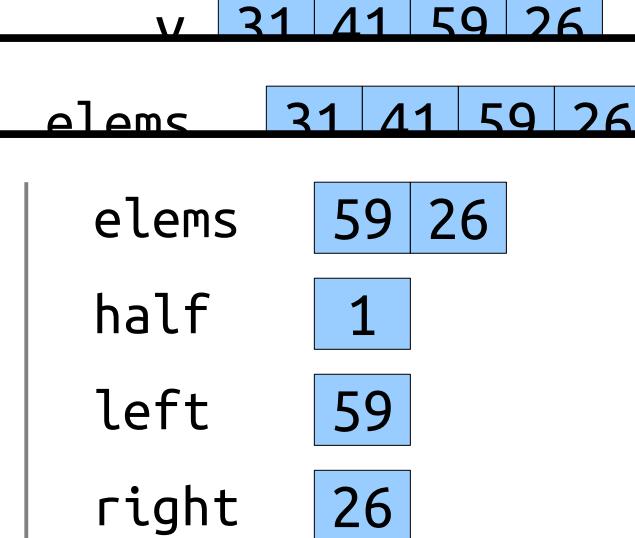
```
int maxOf(const Vector<int>& elems) {  
    if (elems.size() == 1) {  
        return elems[0];  
    } else {  
        int half = elems.size() / 2;  
        Vector<int> left = elems.subList(0, half);  
        Vector<int> right = elems.subList(half);  
        return max(maxOf(left), maxOf(right));  
    }  
}
```



# Tracing the Recursion

i i

```
int maxOf(const Vector<int>& elems) {  
    if (elems.size() == 1) {  
        return elems[0];  
    } else {  
        int half = elems.size() / 2;  
        Vector<int> left = elems.subList(0, half);  
        Vector<int> right = elems.subList(half);  
        return max(maxOf(left), maxOf(right));  
    }  
}
```



# Tracing the Recursion

i

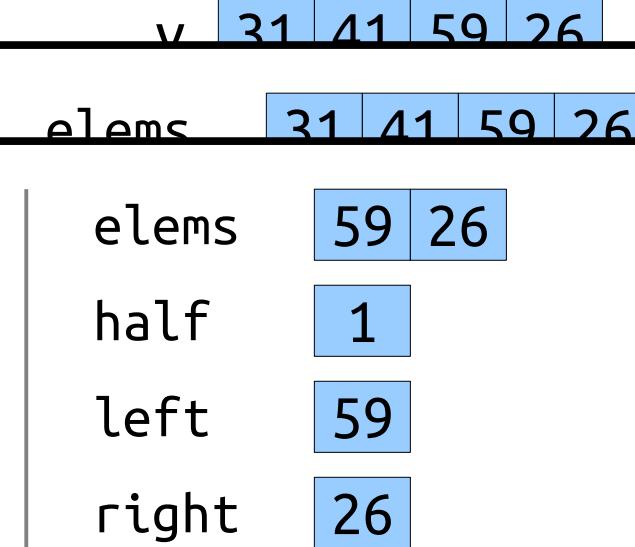
i

```
int maxOf(const Vector<int>& elems) {  
    if (elems.size() == 1) {  
        return elems[0];  
    } else {  
        int half = elems.size() / 2;  
        Vector<int> left  = elems.subList(0, half);  
        Vector<int> right = elems.subList(half);  
        return max(maxOf(left), maxOf(right));  
    }  
}
```



# Tracing the Recursion

```
i i  
int maxOf(const Vector<int>& elems) {  
    if (elems.size() == 1) {  
        return elems[0];  
    } else {  
        int half = elems.size() / 2;  
        Vector<int> left  = elems.subList(0, half);  
        Vector<int> right = elems.subList(half);  
        return max(maxOf(left), maxOf(right));  
    }  
}
```



# Tracing the Recursion

```
int maxOf(const Vector<int>& elems) {
    if (elems.size() == 1) {
        return elems[0];
    } else {
        int half = elems.size() / 2;
        Vector<int> left  = elems.subList(0, half);
        Vector<int> right = elems.subList(half);
        return max(maxOf(left), maxOf(right));
    }
}
```



# Tracing the Recursion

```
int maxOf(const Vector<int>& elems) {
    if (elems.size() == 1) {
        return elems[0];
    } else {
        int half = elems.size() / 2;
        Vector<int> left  = elems.subList(0, half);
        Vector<int> right = elems.subList(half);
        return max(maxOf(left), maxOf(right));
    }
}
```



# Tracing the Recursion

```
int maxOf(const Vector<int>& elems) {
    if (elems.size() == 1) {
        return elems[0];
    } else {
        int half = elems.size() / 2;
        Vector<int> left = elems.subList(0, half);
        Vector<int> right = elems.subList(half);
        return max(maxOf(left), maxOf(right));
    }
}
```



# Tracing the Recursion

```
int maxOf(const Vector<int>& elems) {
    if (elems.size() == 1) {
        return elems[0]; 59
    } else {
        int half = elems.size() / 2;
        Vector<int> left = elems.subList(0, half);
        Vector<int> right = elems.subList(half);
        return max(maxOf(left), maxOf(right));
    }
}
```



# Tracing the Recursion

i

i

```
int maxOf(const Vector<int>& elems) {  
    if (elems.size() == 1) {  
        return elems[0];  
    } else {  
        int half = elems.size() / 2;  
        Vector<int> left  = elems.subList(0, half);  
        Vector<int> right = elems.subList(half);  
        return max(maxOf(left), maxOf(right));  
    }  
}
```

59

v 31 41 59 26

elems 31 41 59 26

elems 59 26

half 1

left 59

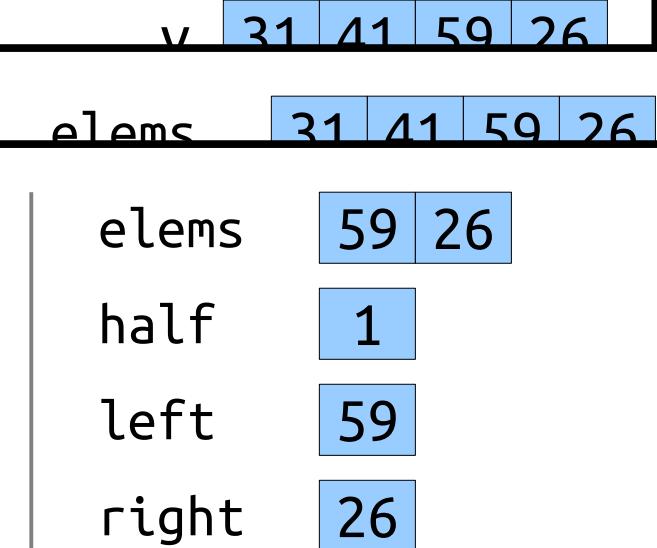
right 26

# Tracing the Recursion

i  
i

```
int maxOf(const Vector<int>& elems) {  
    if (elems.size() == 1) {  
        return elems[0];  
    } else {  
        int half = elems.size() / 2;  
        Vector<int> left = elems.subList(0, half);  
        Vector<int> right = elems.subList(half);  
        return max(maxOf(left), maxOf(right));  
    }  
}
```

59



# Tracing the Recursion

```
int maxOf(const Vector<int>& elems) {  
    if (elems.size() == 1) {  
        return elems[0];  
    } else {  
        int half = elems.size() / 2;  
        Vector<int> left  = elems.subList(0, half);  
        Vector<int> right = elems.subList(half);  
        return max(maxOf(left), maxOf(right));  
    }  
}
```



# Tracing the Recursion

```
int maxOf(const Vector<int>& elems) {  
    if (elems.size() == 1) {  
        return elems[0];  
    } else {  
        int half = elems.size() / 2;  
        Vector<int> left  = elems.subList(0, half);  
        Vector<int> right = elems.subList(half);  
        return max(maxOf(left), maxOf(right));  
    }  
}
```



# Tracing the Recursion

```
int maxOf(const Vector<int>& elems) {  
    if (elems.size() == 1) {  
        return elems[0];  
    } else {  
        int half = elems.size() / 2;  
        Vector<int> left = elems.subList(0, half);  
        Vector<int> right = elems.subList(half);  
        return max(maxOf(left), maxOf(right));  
    }  
}
```



# Tracing the Recursion

```
int maxOf(const Vector<int>& elems) {
    if (elems.size() == 1) {
        return elems[0]; 26
    } else {
        int half = elems.size() / 2;
        Vector<int> left = elems.subList(0, half);
        Vector<int> right = elems.subList(half);
        return max(maxOf(left), maxOf(right));
    }
}
```



# Tracing the Recursion

i

i

```
int maxOf(const Vector<int>& elems) {  
    if (elems.size() == 1) {  
        return elems[0];  
    } else {  
        int half = elems.size() / 2;  
        Vector<int> left = elems.subList(0, half);  
        Vector<int> right = elems.subList(half);  
        return max(maxOf(left), maxOf(right));  
    }  
}
```

59

26

v 31 41 59 26

elems 31 41 59 26

elems 59 26

half 1

left 59

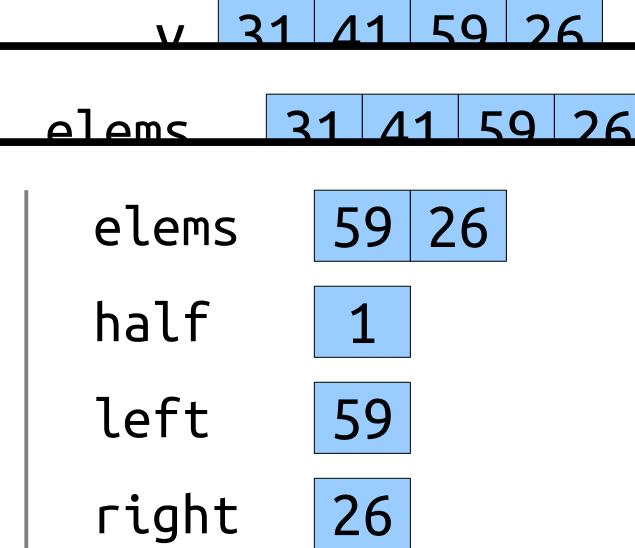
right 26

# Tracing the Recursion

i i

```
int maxOf(const Vector<int>& elems) {  
    if (elems.size() == 1) {  
        return elems[0];  
    } else {  
        int half = elems.size() / 2;  
        Vector<int> left  = elems.subList(0, half);  
        Vector<int> right = elems.subList(half);  
        return max(maxOf(left), maxOf(right));  
    }  
}
```

59            26



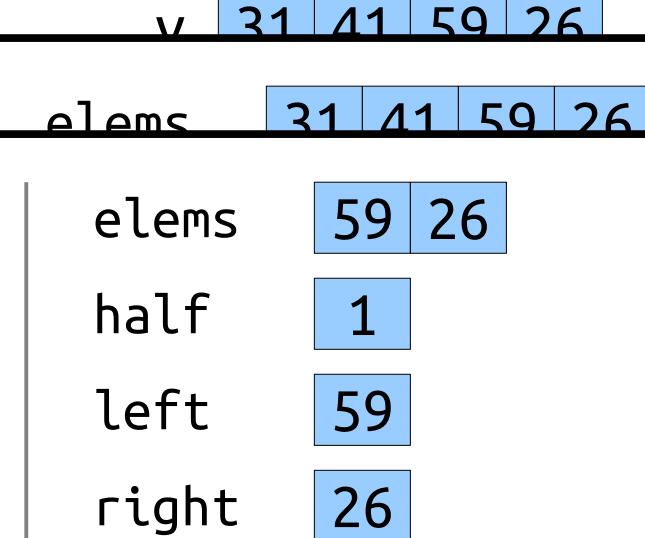
# Tracing the Recursion

i

i

```
int maxOf(const Vector<int>& elems) {  
    if (elems.size() == 1) {  
        return elems[0];  
    } else {  
        int half = elems.size() / 2;  
        Vector<int> left  = elems.subList(0, half);  
        Vector<int> right = elems.subList(half);  
        return max(maxOf(left), maxOf(right));  
    }  
}
```

59

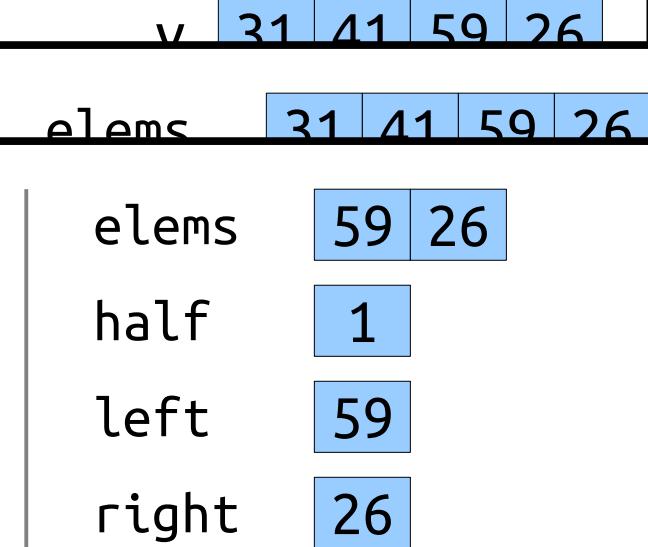


# Tracing the Recursion

i i

```
int maxOf(const Vector<int>& elems) {  
    if (elems.size() == 1) {  
        return elems[0];  
    } else {  
        int half = elems.size() / 2;  
        Vector<int> left = elems.subList(0, half);  
        Vector<int> right = elems.subList(half);  
        return max(maxOf(left), maxOf(right));  
    }  
}
```

59



# Tracing the Recursion

i

```
int maxOf(const Vector<int>& elems) {  
    if (elems.size() == 1) {  
        return elems[0];  
    } else {  
        int half = elems.size() / 2;  
        Vector<int> left = elems.subList(0, half);  
        Vector<int> right = elems.subList(half);  
        return max(maxOf(left), maxOf(right));  
    }  
}
```

**41**      **59**

v 31 41 59 26

elems	31 41 59 26
half	2
left	31 41
right	59 26

# Tracing the Recursion

i

```
int maxOf(const Vector<int>& elems) {  
    if (elems.size() == 1) {  
        return elems[0];  
    } else {  
        int half = elems.size() / 2;  
        Vector<int> left = elems.subList(0, half);  
        Vector<int> right = elems.subList(half);  
        return max(maxOf(left), maxOf(right));  
    }  
}
```

41

59

v 31 41 59 26

elems	31 41 59 26
half	2
left	31 41
right	59 26

# Tracing the Recursion

i

```
int maxOf(const Vector<int>& elems) {  
    if (elems.size() == 1) {  
        return elems[0];  
    } else {  
        int half = elems.size() / 2;  
        Vector<int> left = elems.subList(0, half);  
        Vector<int> right = elems.subList(half);  
        return max(maxOf(left), maxOf(right));  
    }  
}
```

v 31 41 59 26

elems	31	41	59	26
half	2			
left	31	41		
right	59	26		

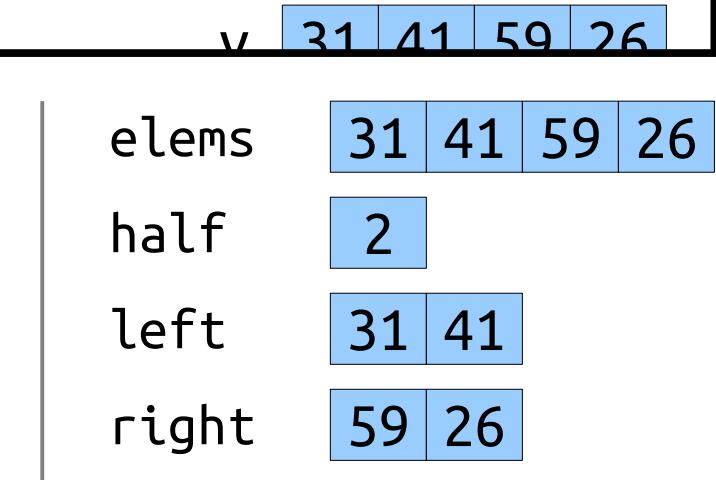
59

# Tracing the Recursion

i

```
int maxOf(const Vector<int>& elems) {  
    if (elems.size() == 1) {  
        return elems[0];  
    } else {  
        int half = elems.size() / 2;  
        Vector<int> left = elems.subList(0, half);  
        Vector<int> right = elems.subList(half);  
        return max(maxOf(left), maxOf(right));  
    }  
}
```

59



# Tracing the Recursion

v 31 41 59 26

```
int main() {  
    Vector<int> v = { 31, 41, 59, 26 };  
    cout << maxOf(v) << endl;  
    return 0; 59  
}
```